



Discrete Event Simulation

IN2045

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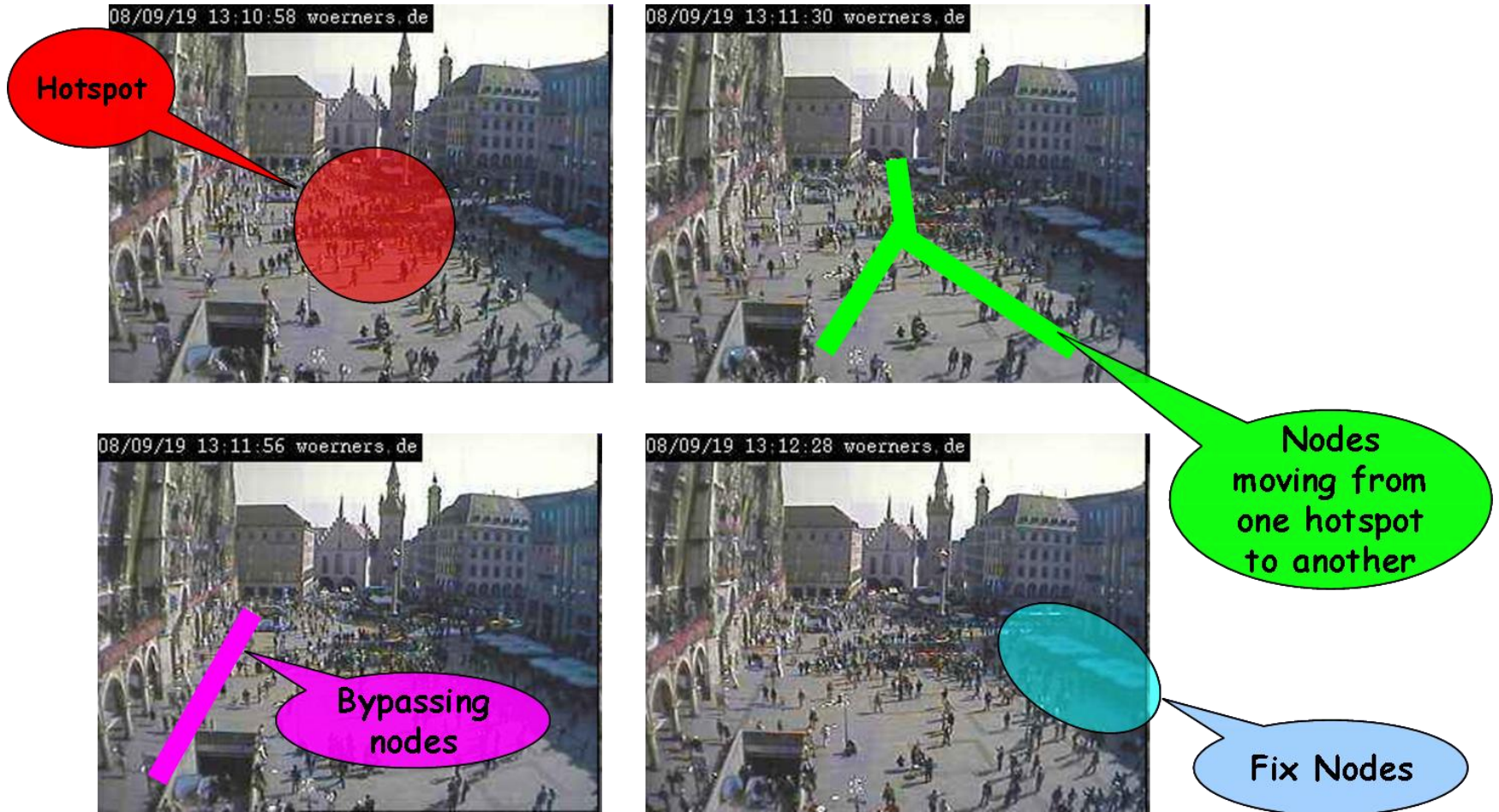
Topics

- ❑ Mobility in General
 - Realistic Movement
 - Human Mobility Pattern
- ❑ Visualization
 - Density
 - Speed Histograms
- ❑ Characteristics of Mobility Pattern
 - Link Duration, Transient Phase, Node Distribution, Speed Distribution, Correlated Movement
- ❑ Synthetic Mobility Models
 - Random Waypoint
 - Random Direction
 - Random Walk
 - Levi-Flight
 - Brownian Motion
 - Group Mobility





□ What is (random) mobility?





□ Why simulate mobility?

- Improvements in technology enable new technologies and result in cheaper hardware prices
- Number of powerful mobile devices increases very quickly (Smartphones with high data rate interfaces)
- Number of applications for mobile devices increases
- Impact on the system performance can often not be predicted in advance

□ Impact on wireless networks:

- Topology depends on the user mobility
- Routing protocols have to react on topology changes (link duration)
- Frequent changes of the user density result in variation of the interference
- May lead to a collapse of the network if the applied protocols are not optimized (overhead, dissemination of outdated information)
- Enables new information dissemination strategies (Delay-Tolerant-Networking)

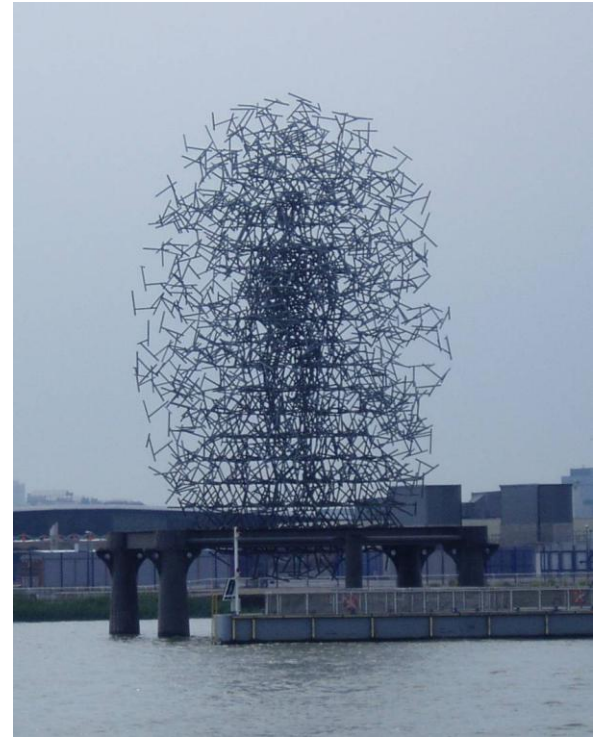


□ What is realistic movement?

- Random movement?
- Correlated movement?
- Movement of humans?

□ Mobility Pattern

- Pedestrians
- Police patrol / avalanche rescue
- Cars on the road
- Trains
- Air planes
- Animals (hunter and prey)
- Constraint by obstacles / infrastructure

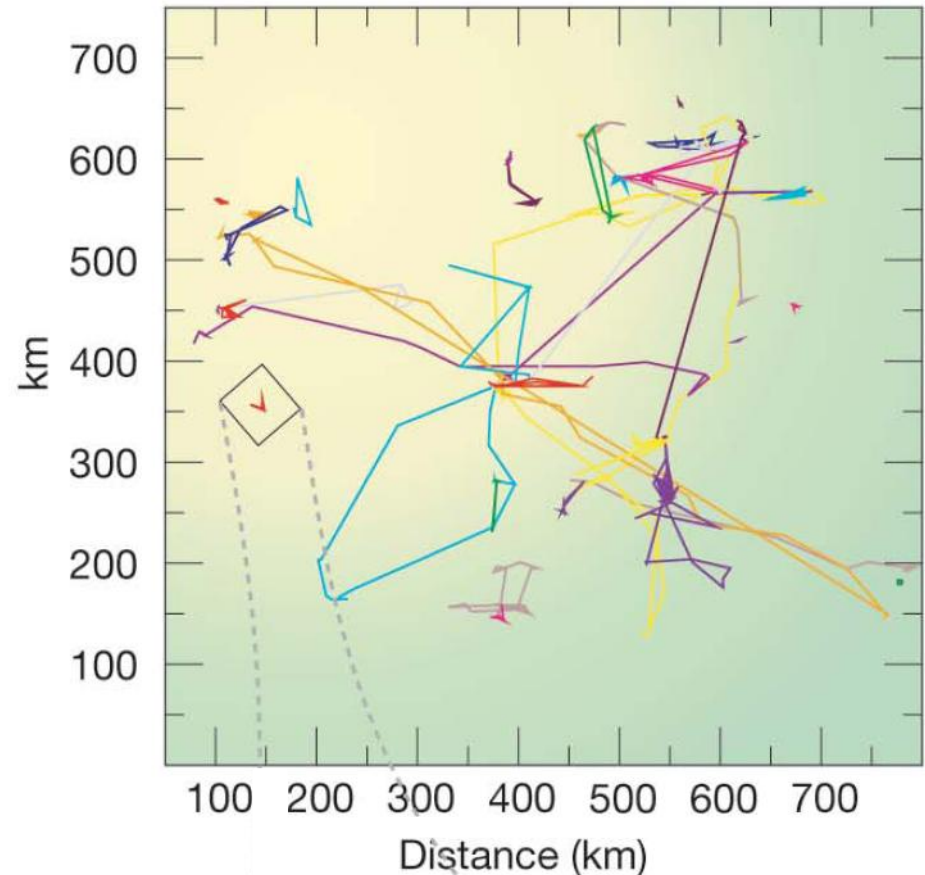


Antony Gormley's *Quantum Cloud* sculpture in London
(based on a random walk model)



□ Human mobility pattern:

- Short-term and long-term characteristics
- Often approximated by the levy-flight synthetic mobility model which is derived from the random walk model
- High probability that the next position is close to the previous one
- Low probability that the individual travels long distances
- High variation between different individuals

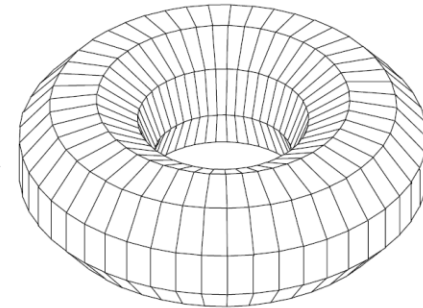
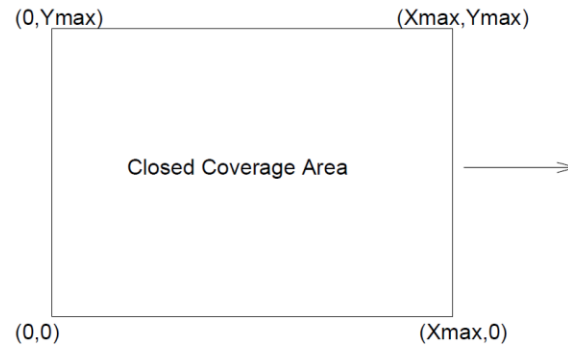
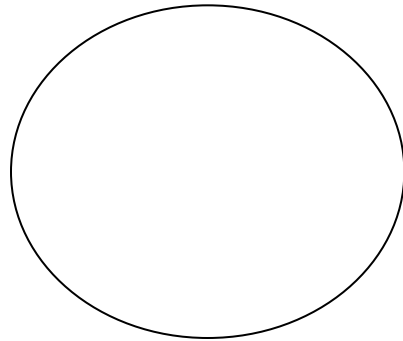


González, M. C.; Hidalgo, C. A. & Barabási, A.
Understanding Individual Human Mobility Patterns
Nature, 2008, 453, 779-782



□ Simulation

- Area (circle, square, rectangle, sphere, torus, ...)

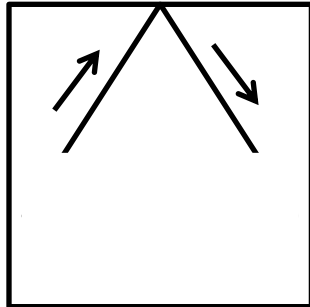


- Long-term simulation
 - Transient phase of the model
 - Node distribution
 - Speed distribution
 - Partitioning of the network

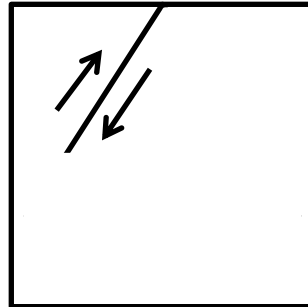


Simulation

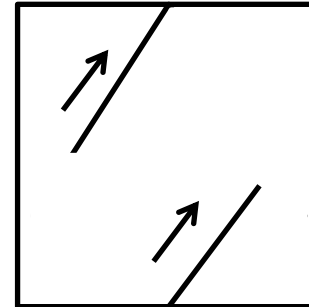
- Bouncing rule:



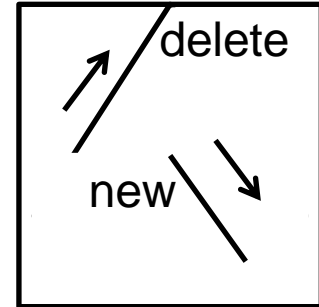
bounce



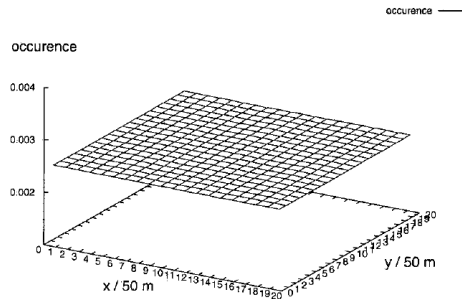
reflect



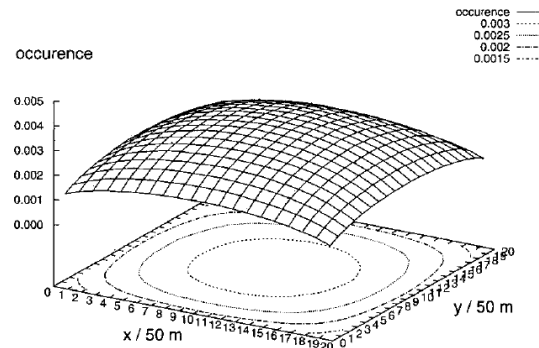
wrap-around



delete & replace



f) Random direction model with “bounce” or “wrap-around”



Random direction model with “delete and replace”

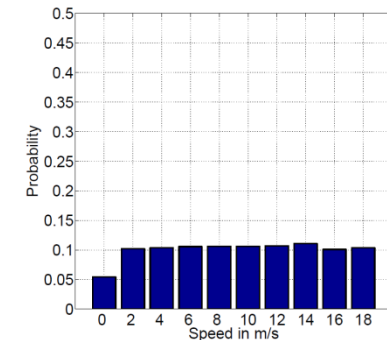
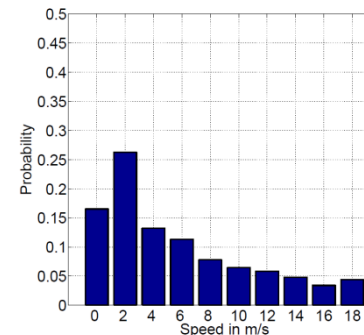
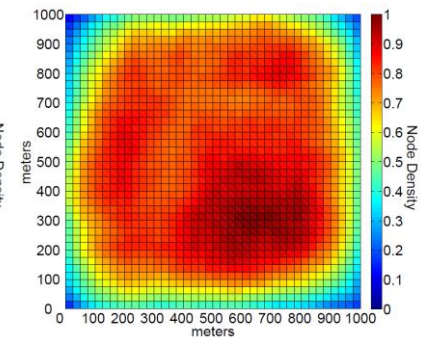
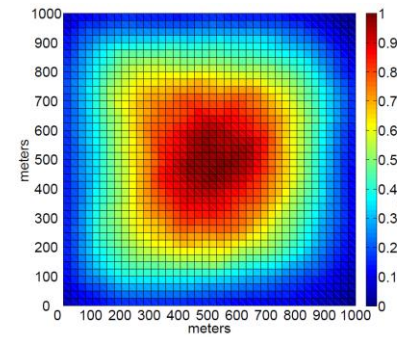
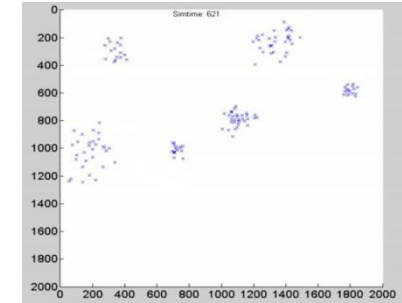
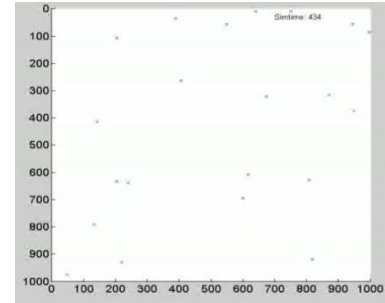
Article (Bettstetter2001)
 Bettstetter, C.
 Mobility Modeling in Wireless Networks: Categorization, Smooth Movement, and Border Effects
ACM SIGMOBILE Mobile Computing and Communications Review,
 ACM, 2001, 5, 55-66

Node Distribution changes depending on the applied bouncing rule



□ Visualization

- Movement (Debugging)
 - Debugging
 - Detect correlated movement
 - Evaluation
- Density
 - Spatial node distribution
 - Border effects
 - Estimation of transient phase
- Histograms
 - Node speed distribution
 - Link duration
 - Estimation of transient phase





□ Characteristics:

- Link duration
 - Important wireless communication parameter
 - Represents the time interval during which two nodes are able to communicate with each other

- Transient phase
 - One or more parameters change significantly during this phase
 - Duration of the transient phase varies between different synthetic mobility models

- Spatial node distribution
 - Depends on the mobility model
 - Often affected by the shape of the simulation plane
 - Influenced by the applied bouncing rule



□ Characteristics:

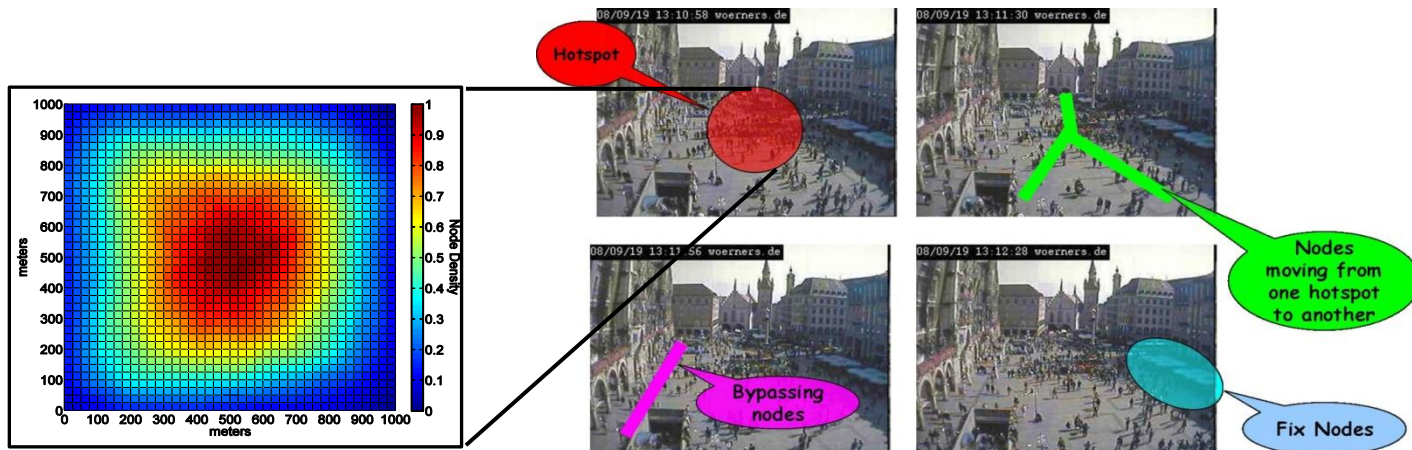
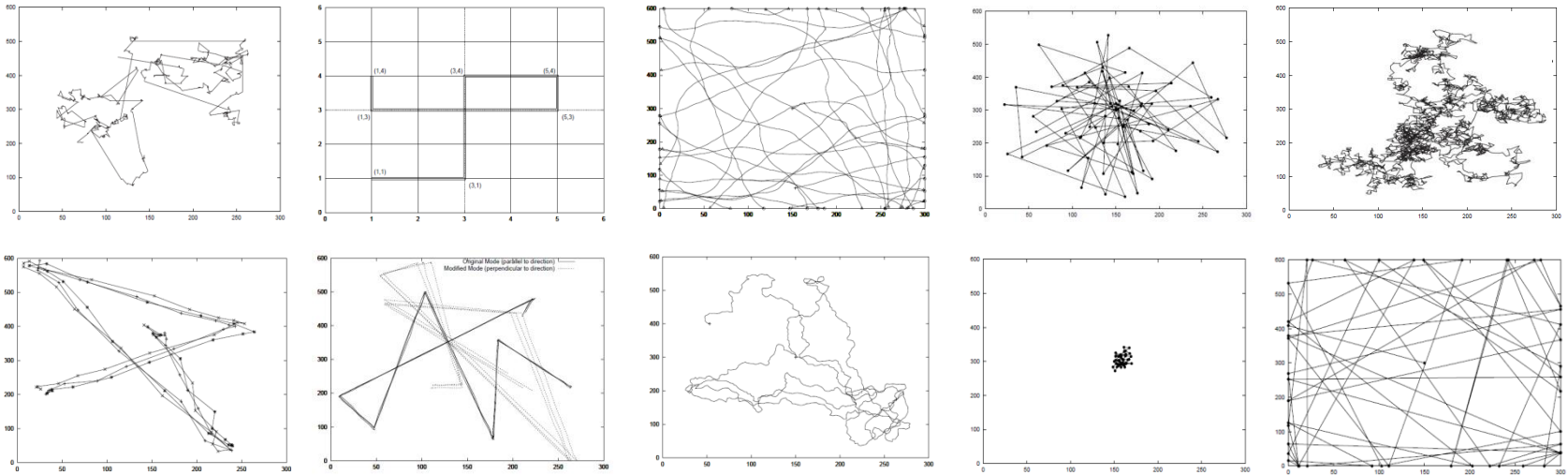
- Speed distribution
 - Good indicator for the duration of the transient phase
 - Mainly influenced by the following parameters:
 - Time-based or distance-based movement decision
 - Pause time
 - Shape of the simulation plane

- Correlated / Constraint movement
 - Each move is affected by the previous one
 - Objects may interact with each other

- Group mobility
 - The movement of objects is a composition of the movement of the individual and a common (group leader) object



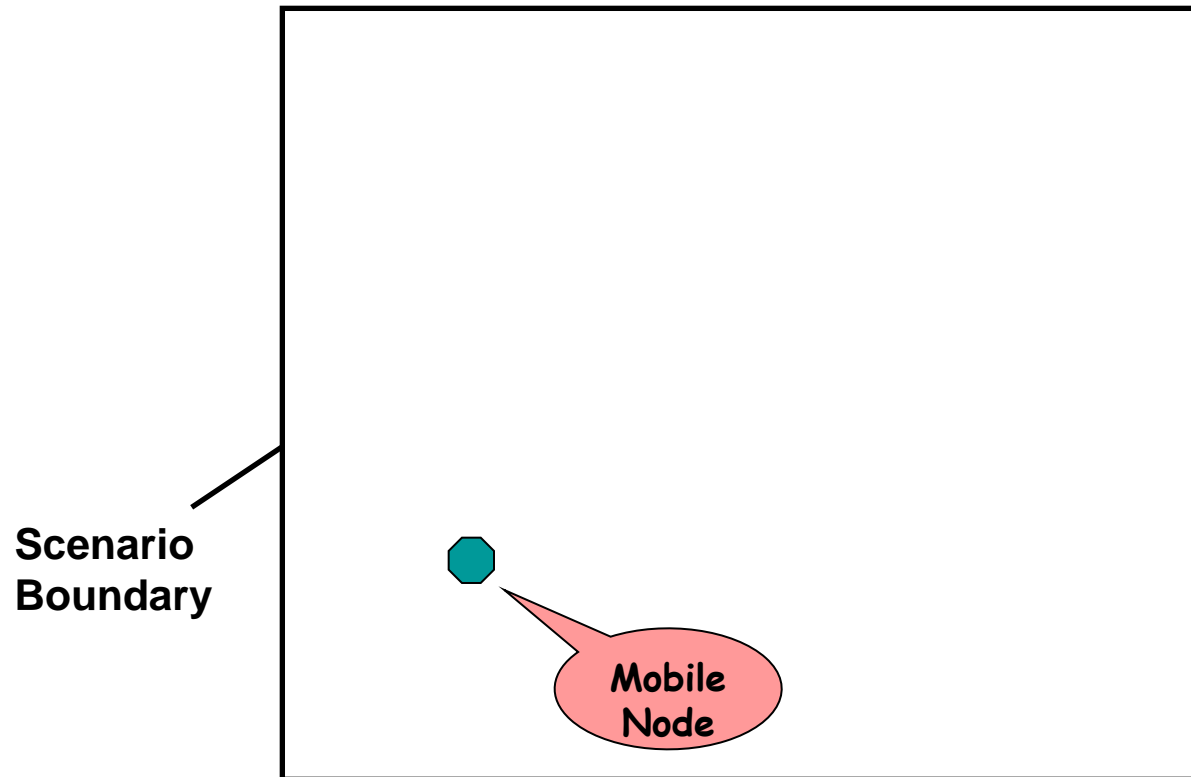
□ Synthetic Mobility Models





□ Random Waypoint

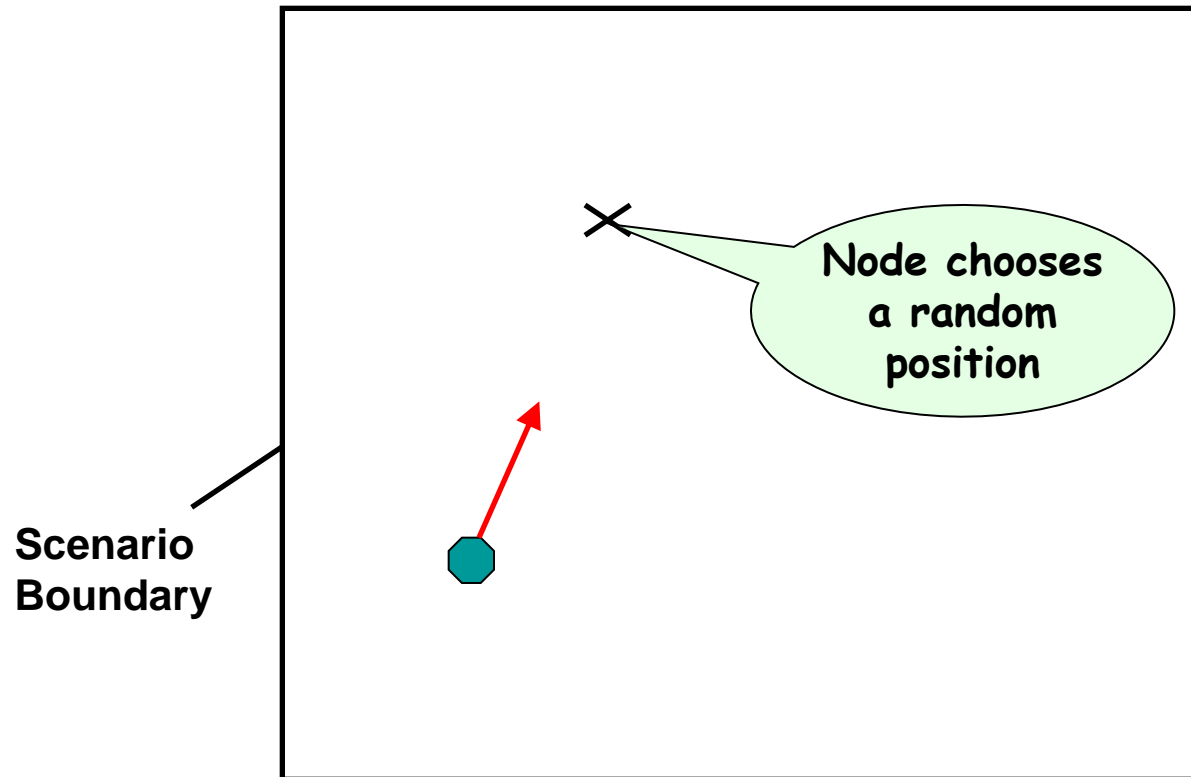
Algorithm:





□ Random Waypoint

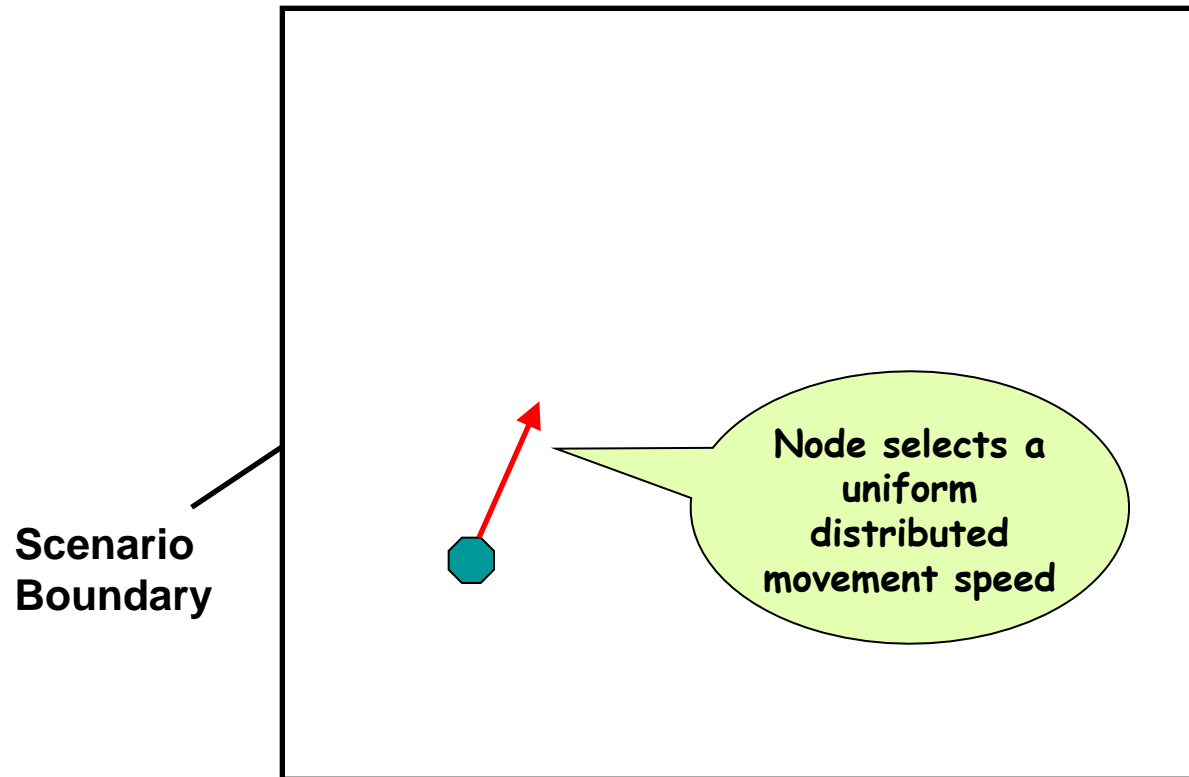
Algorithm:





□ Random Waypoint

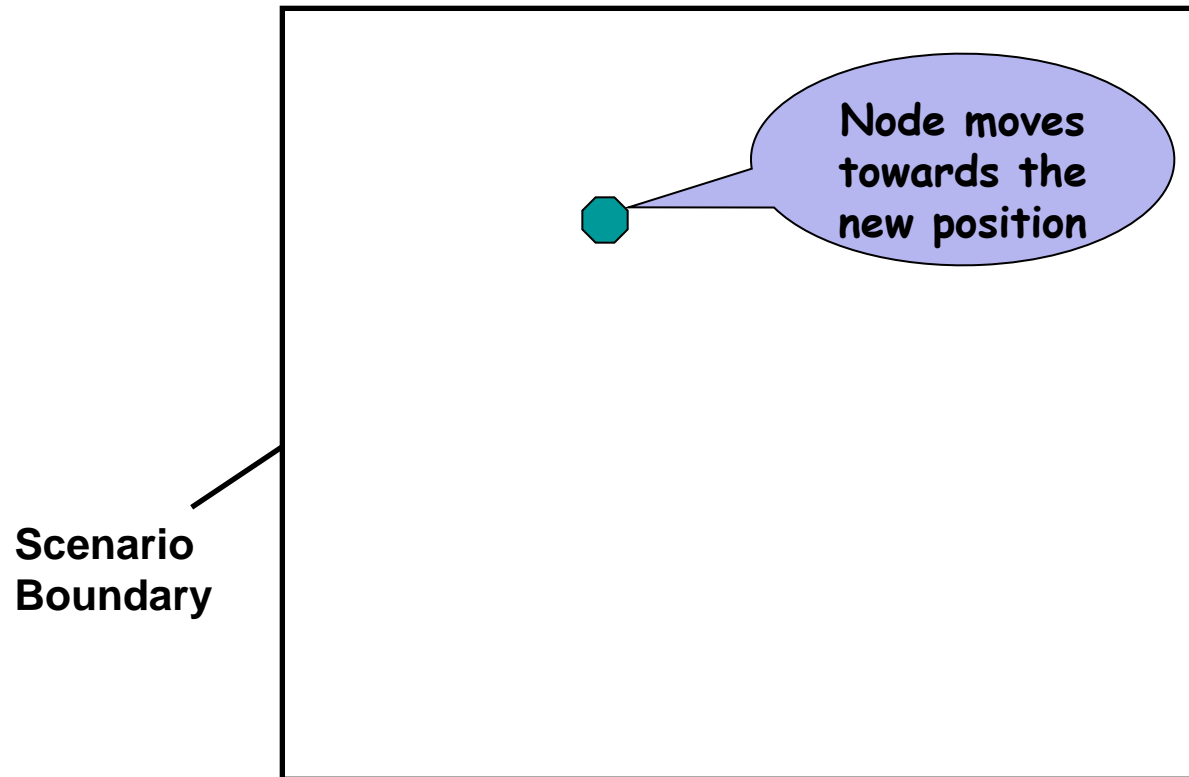
Algorithm:





□ Random Waypoint

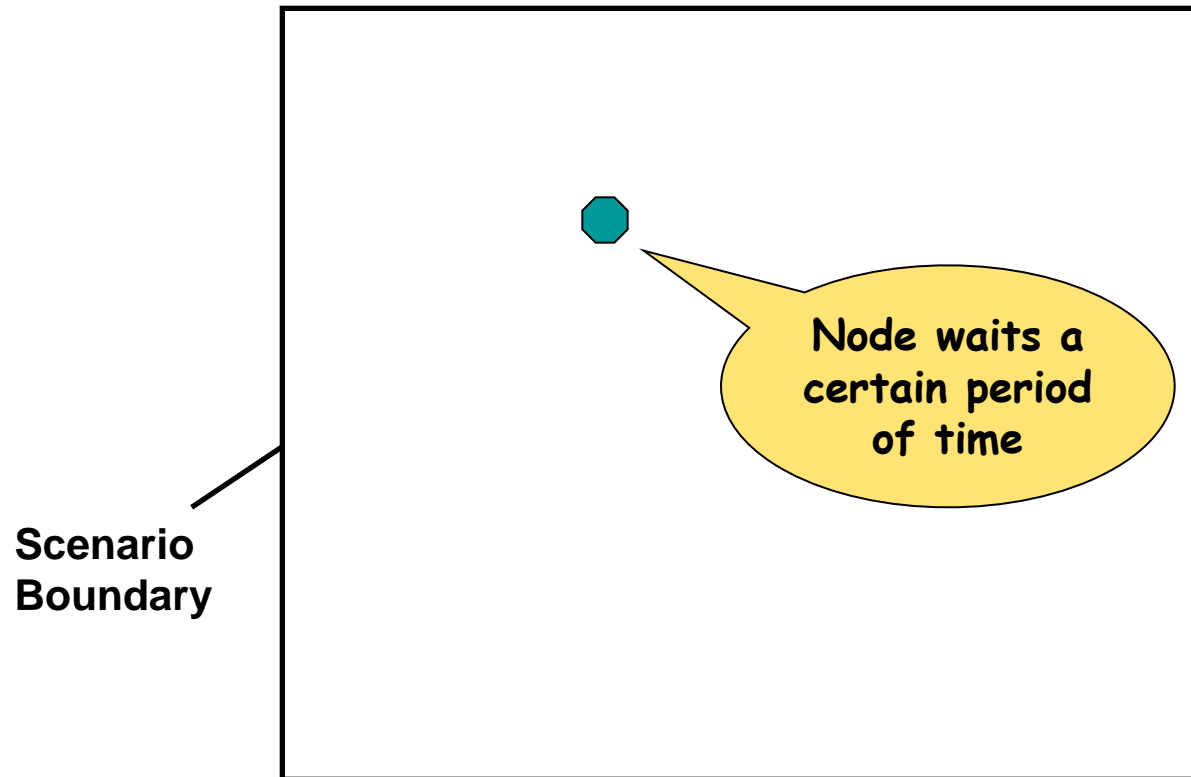
Algorithm:





□ Random Waypoint

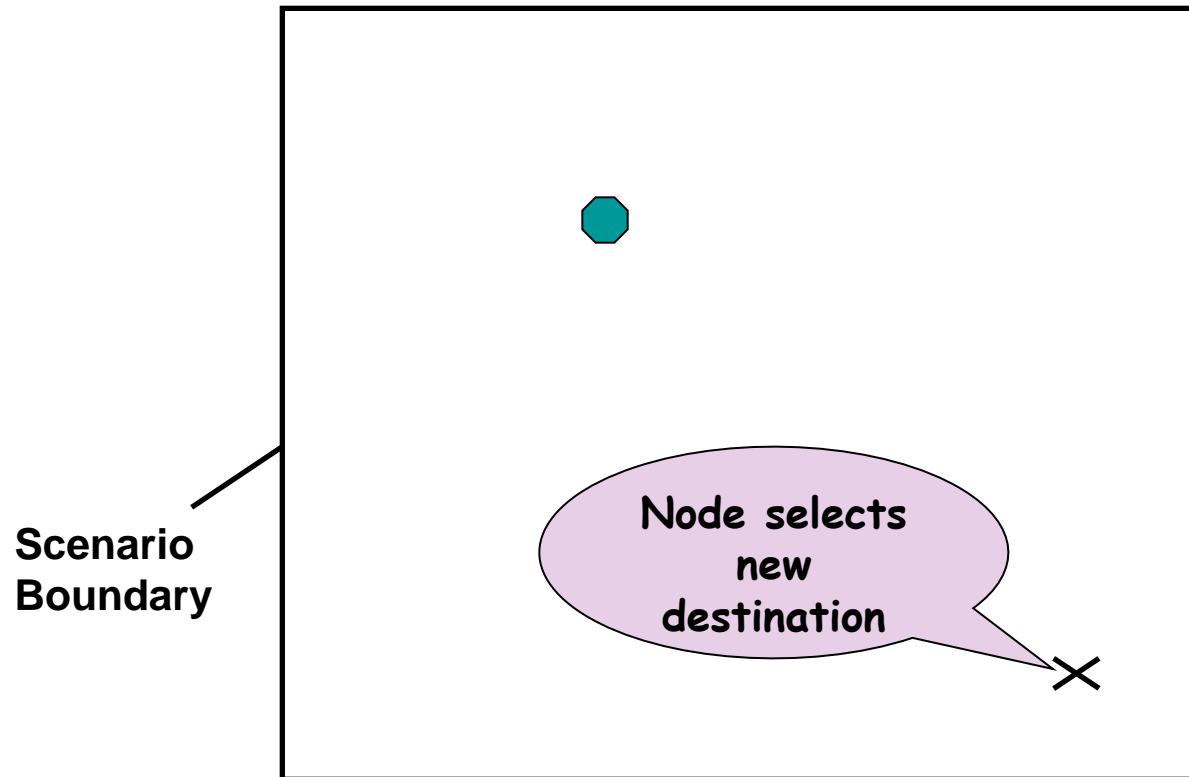
Algorithm:





□ Random Waypoint

Algorithm:





□ Random Waypoint

Algorithm:

Step 1: Select a random destination within the scenario

Step 2: Select a random speed $speed \in [speed_{Min}; speed_{Max}]$


Step 3: Move until the destination is reached

Step 4: Wait a random period of time $pause \in [0; pause_{Max}]$

Step 5: Go to step 1



□ Random Waypoint

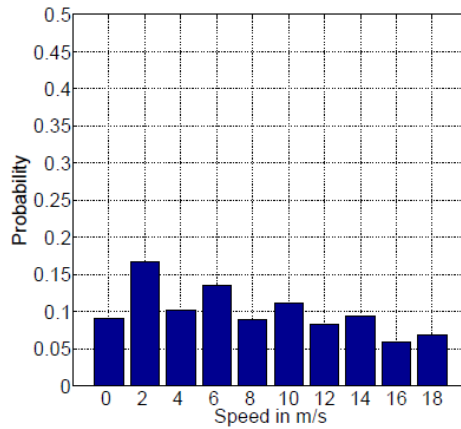
- Characteristics:
 - Node density decreases towards the border
 - Highest node density in the center
 - The fraction of slow moving nodes increases over time
 - Long transient phase
 - Individual nodes recognize density waves while moving through the center
 - Average node speed decreases over time  speed decay problem

- Advantage:
 - Simple to implement
 - Challenging mobility due to changing node density

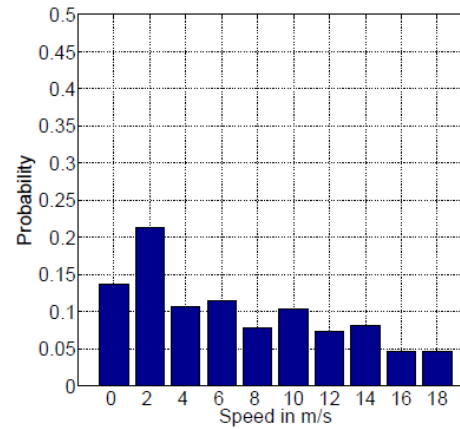
- Disadvantage:
 - Has to be configured carefully (Minimum speed and pause duration)
 - Movement affected by the shape of the simulation plane



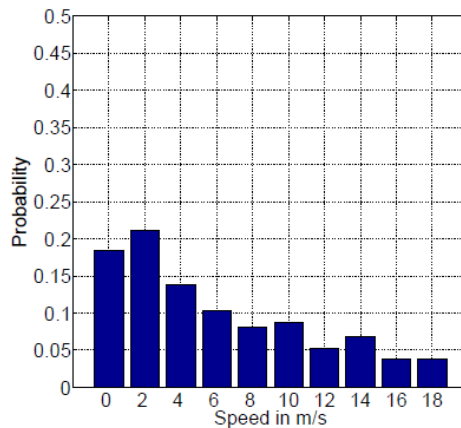
- Random Waypoint
 - Node speed distribution:



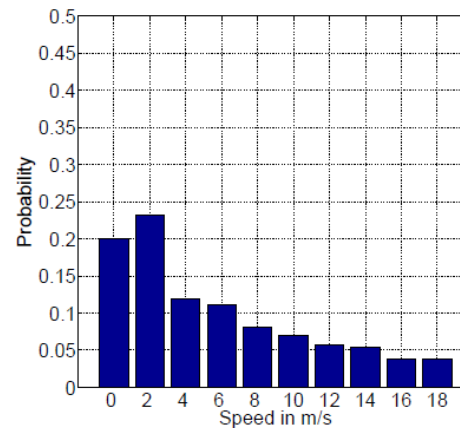
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds

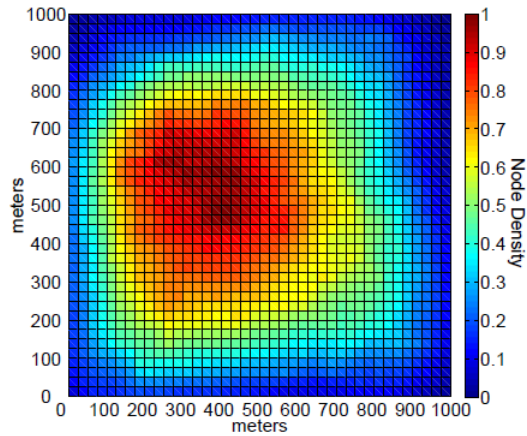


(d) 800 Seconds

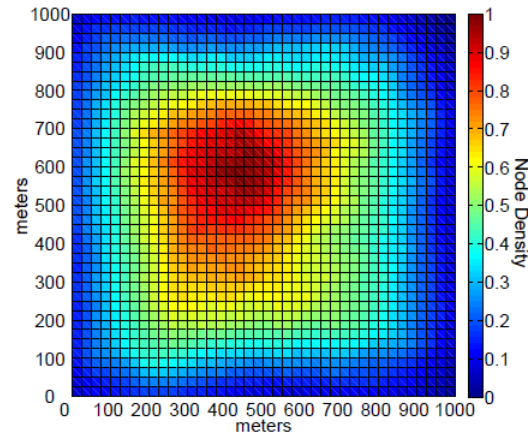


□ Random Waypoint

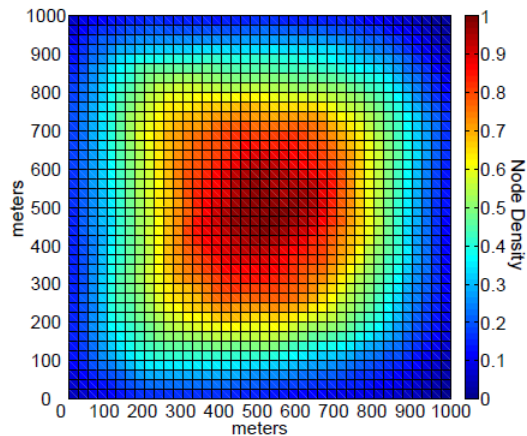
- Node density:



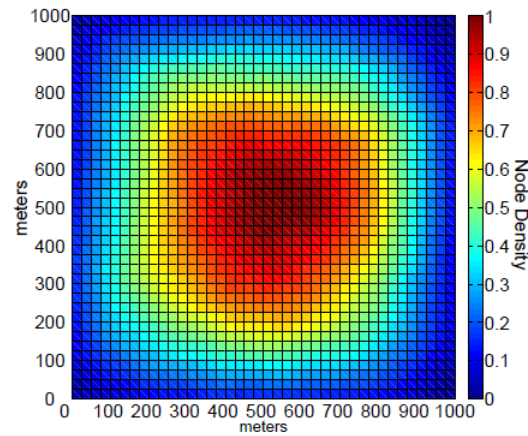
(a) 100 Seconds



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(c) 400 Seconds

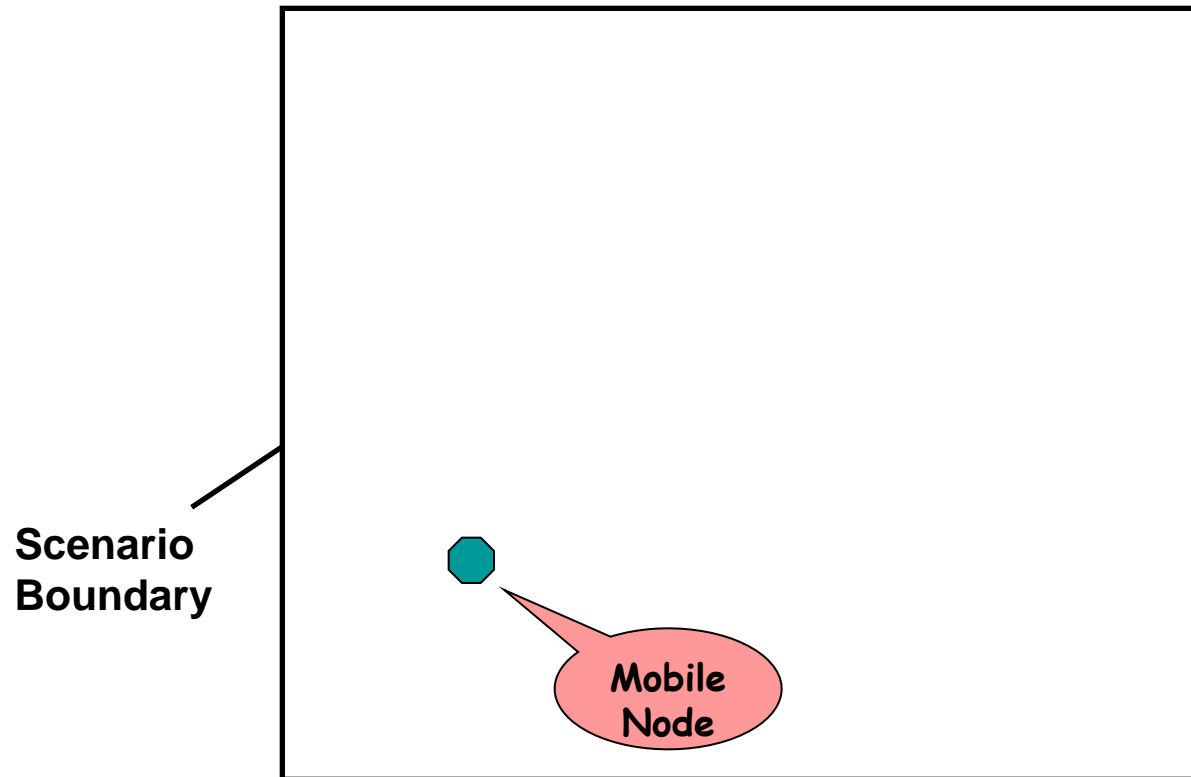


(d) 800 Seconds



□ Random Direction

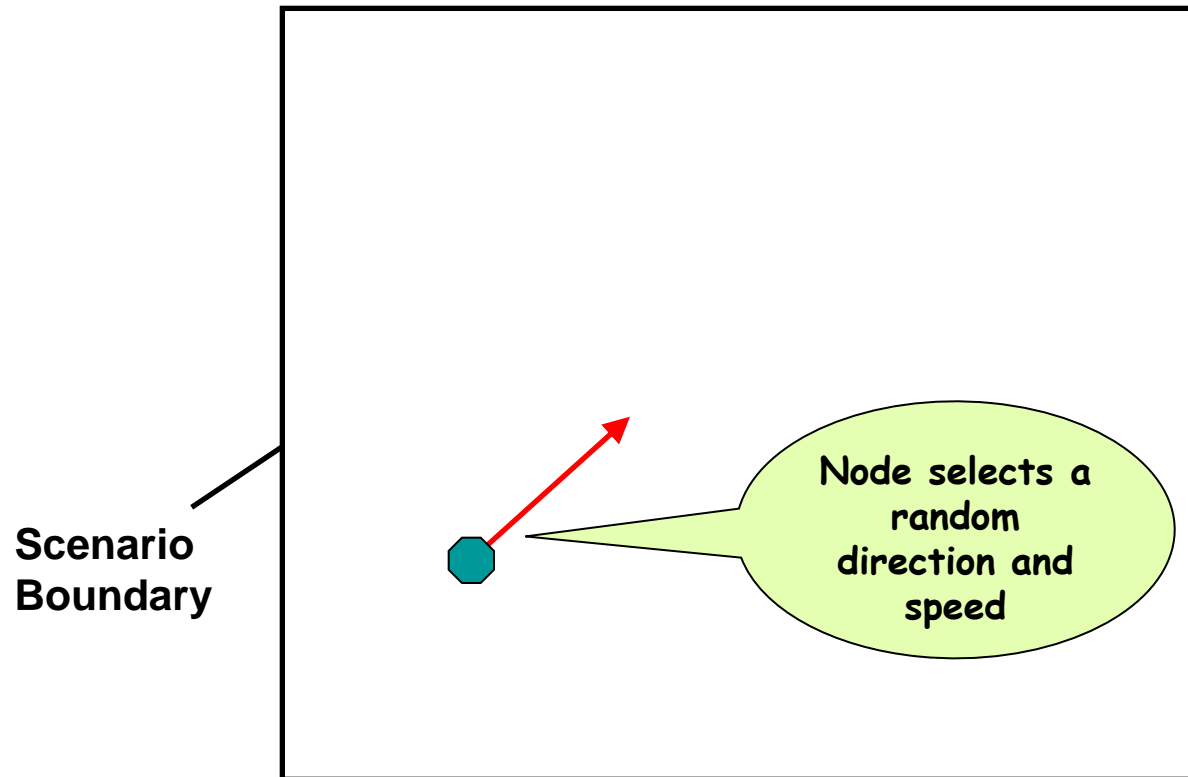
Algorithm:





□ Random Direction

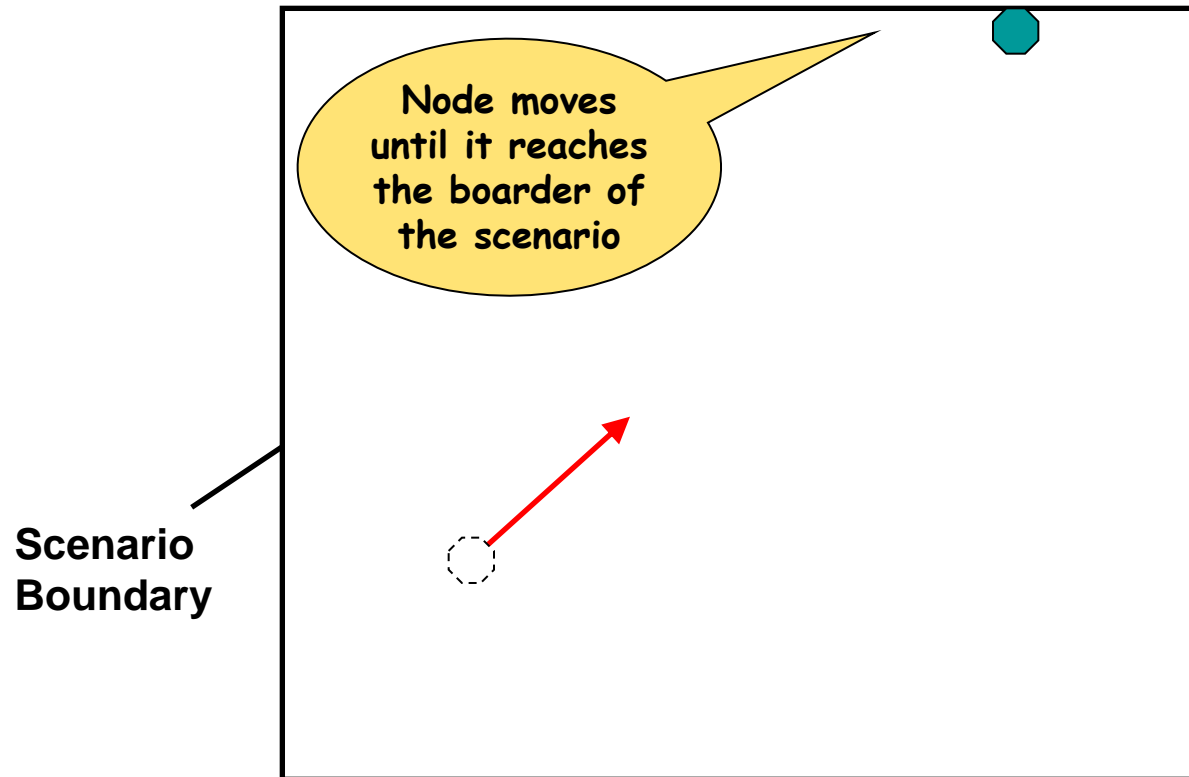
Algorithm:





□ Random Direction

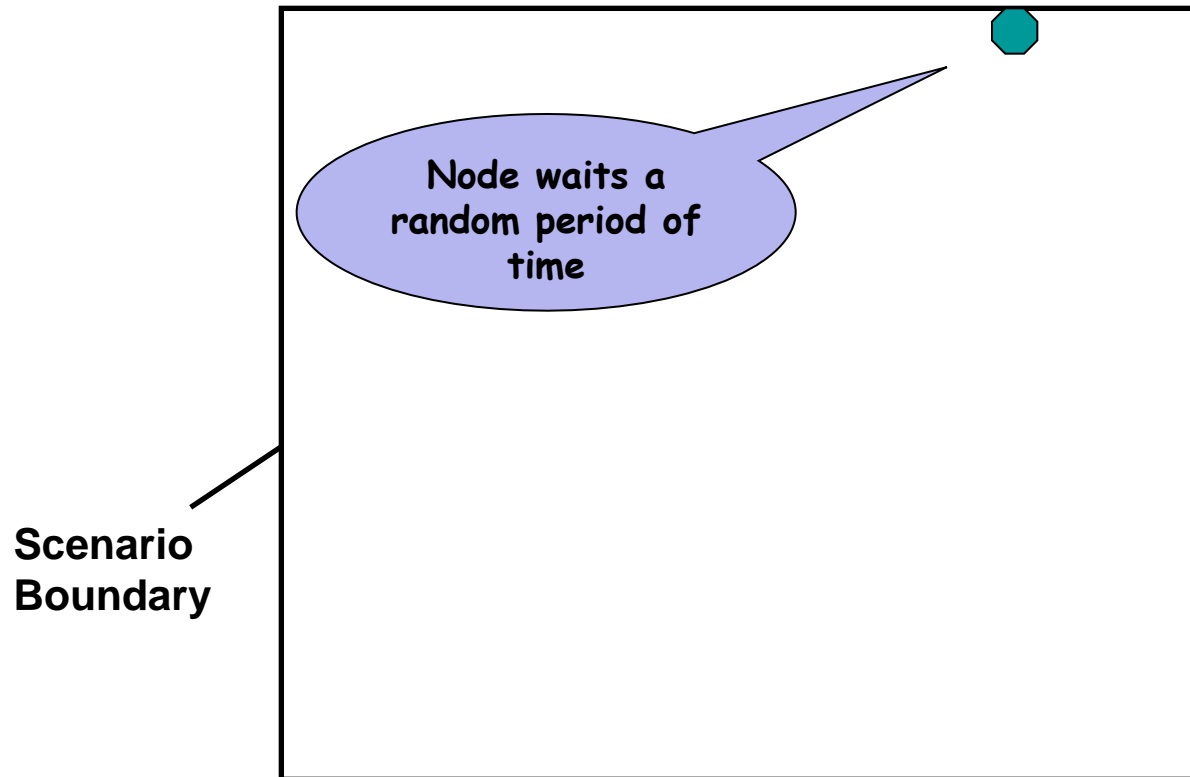
Algorithm:





□ Random Direction

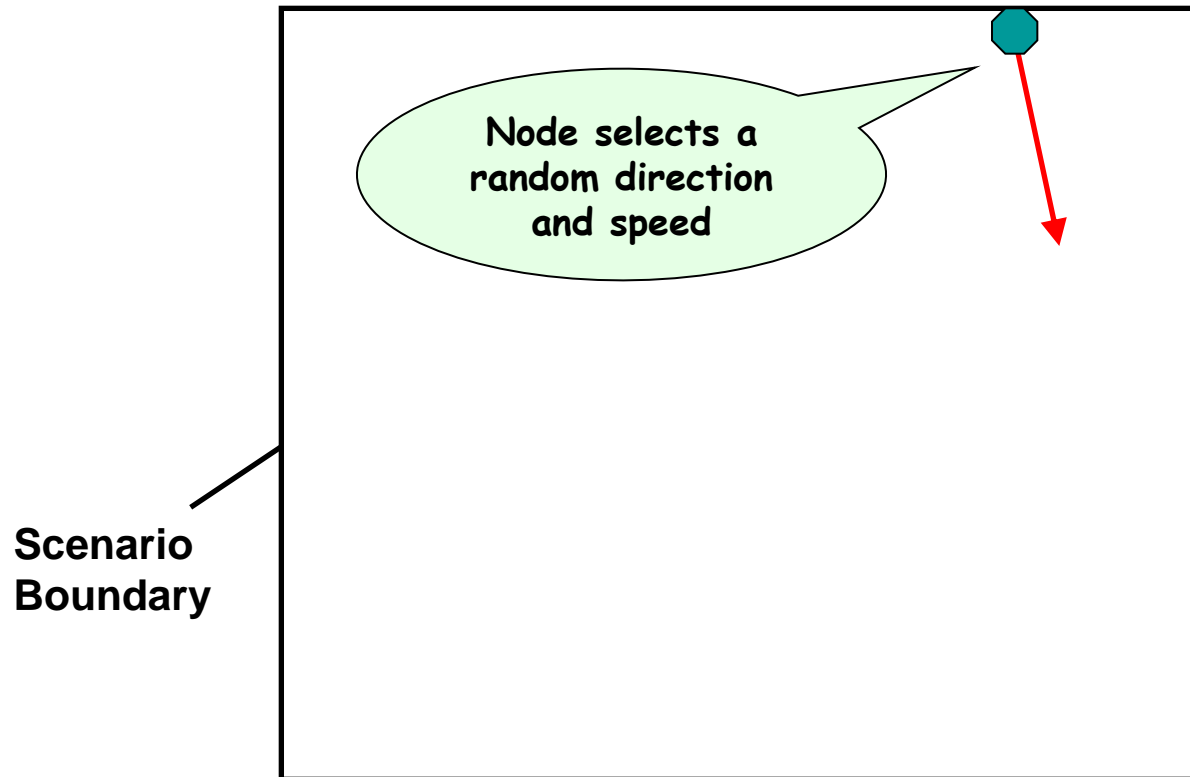
Algorithm:





□ Random Direction

Algorithm:





□ Random Direction

Algorithm:

- Step 1: Select a random direction $direction \in [0; 2\pi]$
(such that the node does not leave the scenario)
- Step 2: Select a random speed $speed \in [speed_{Min}; speed_{Max}]$
- Step 3: Move until the border of the scenario is reached
- Step 4: Bouncing rule:
 - a. Wait a random period of time $pause \in [0; pause_{Max}]$
 - b. Delete the node and replace it with a new node
in the center or at a random position
 - c. Place the node at the opposite side of the
simulation plane
- Step 5: Go to step 1



□ Random Direction

- Characteristics:
 - Node density increases towards the border
 - Highest node density at the border and in the corners
 - The fraction of slow moving nodes increases over time
 - Short transient phase
 - Nodes in the corner are strongly affected by the applied bouncing rule

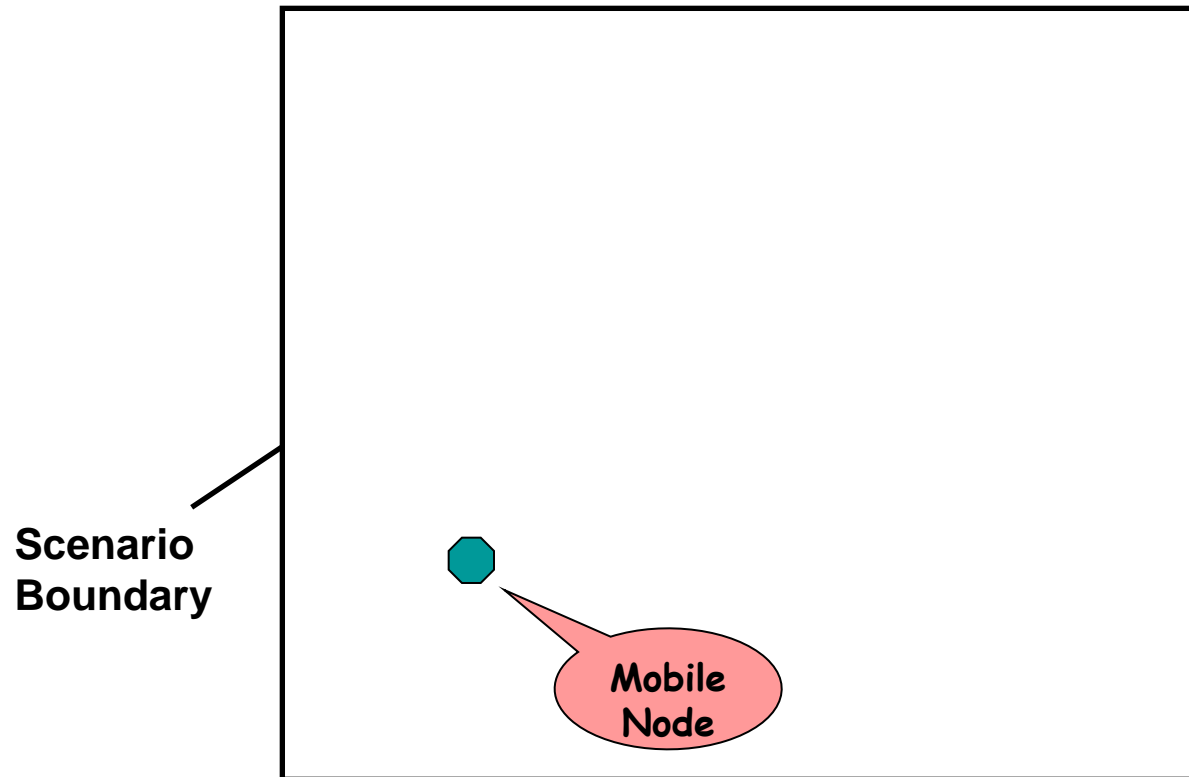
- Advantage:
 - Simple to implement
 - Uniform distributed node density (depends on the bouncing rule)

- Disadvantage:
 - Has to be configured carefully (Minimum speed and pause duration)
 - Movement affected by the shape of the simulation plane
 - Large impact of the bouncing rule



- Random Walk (time-based / distance-based)

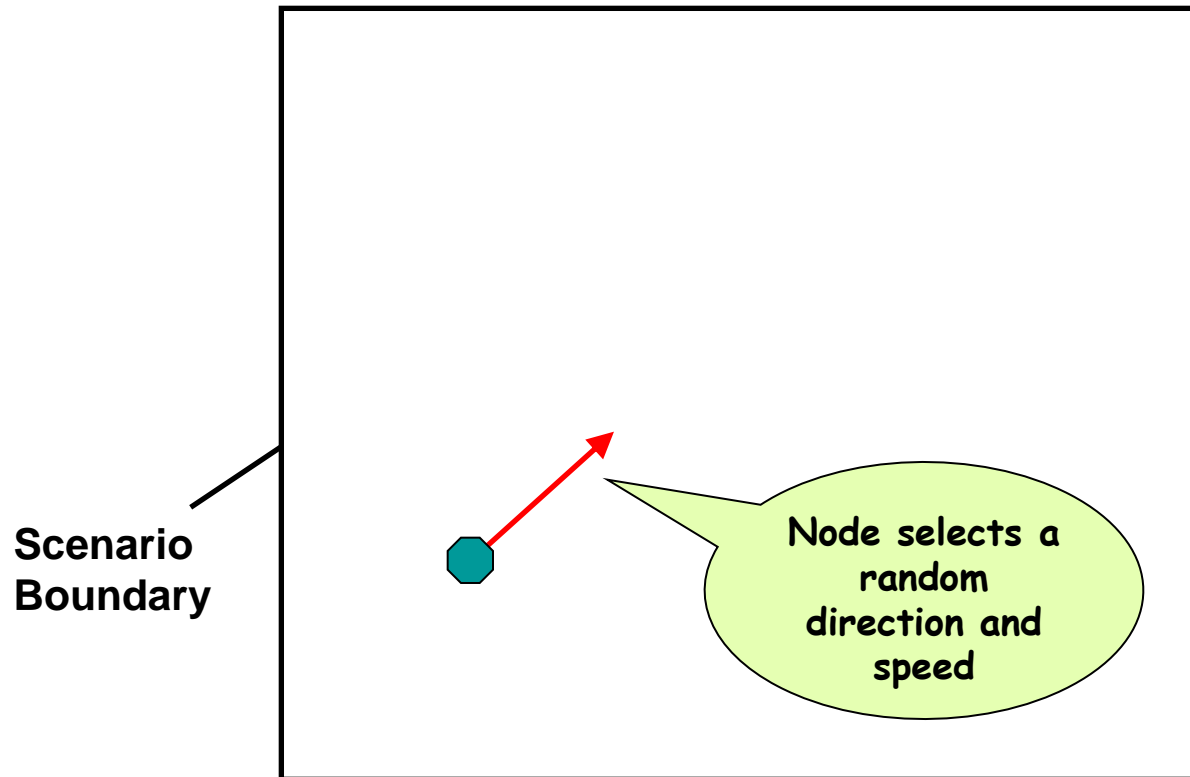
Algorithm:





- Random Walk (time-based / distance-based)

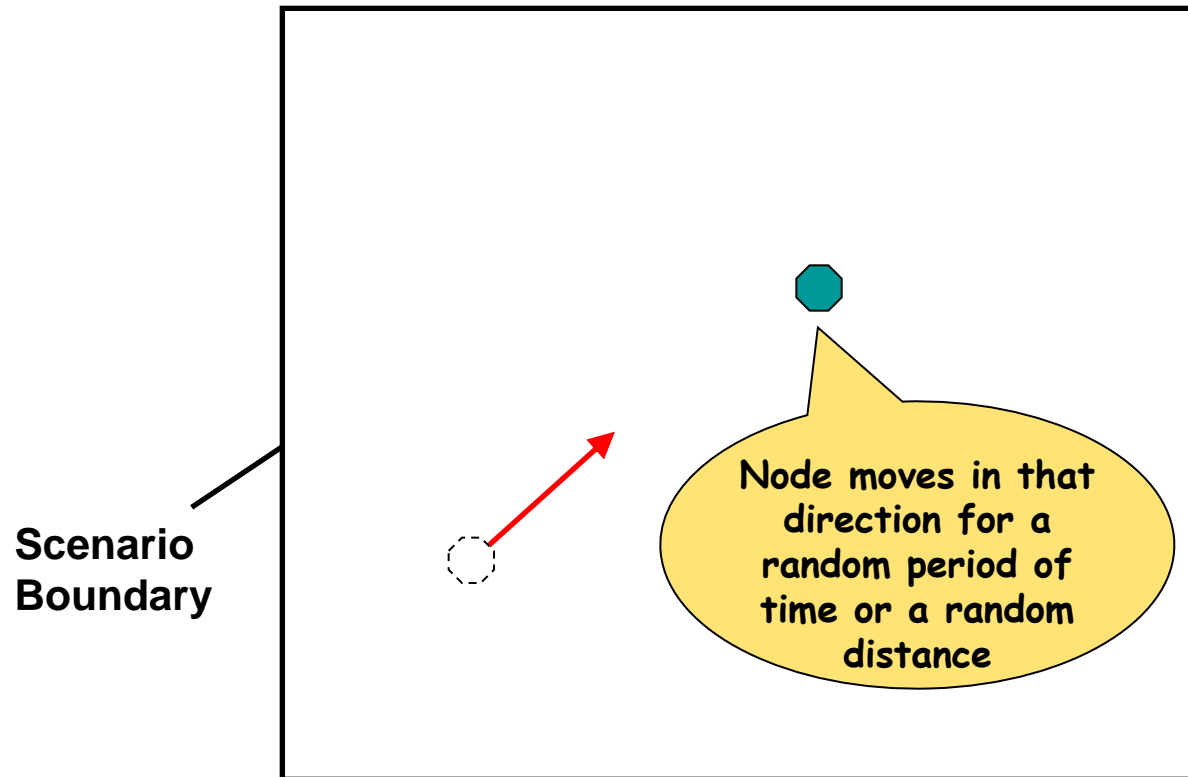
Algorithm:





- Random Walk (time-based / distance-based)

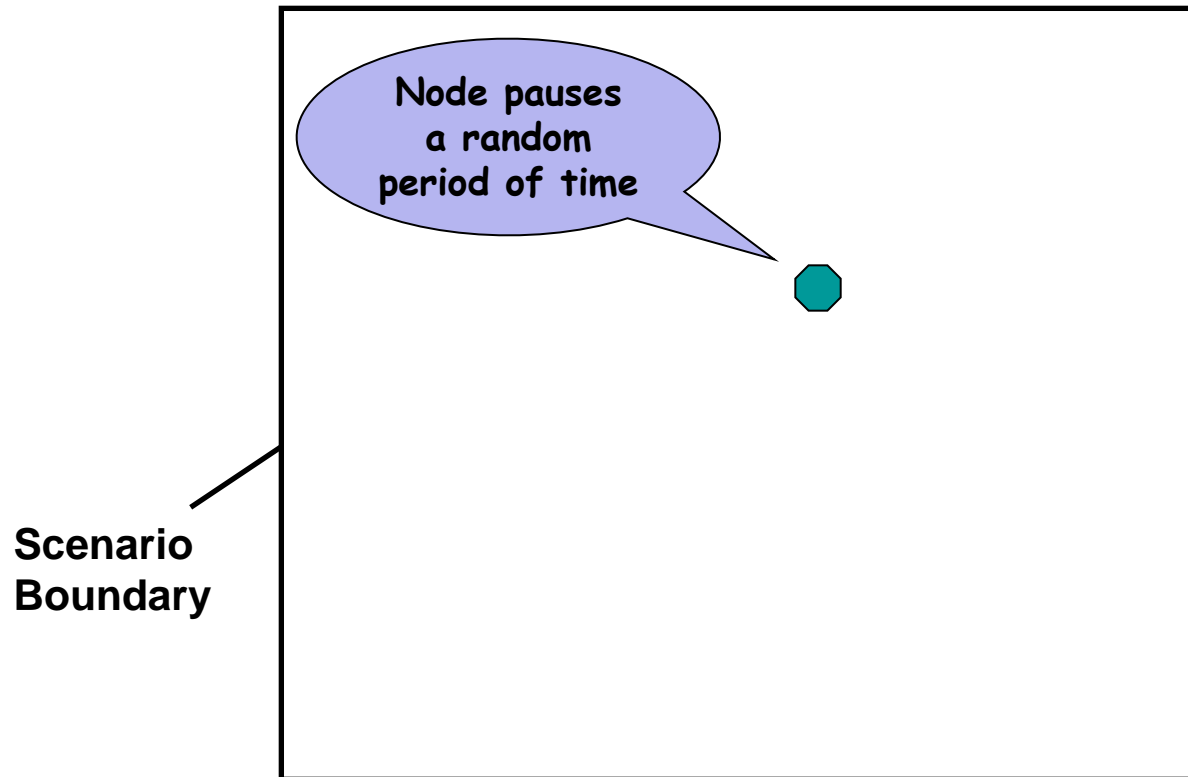
Algorithm:





- Random Walk (time-based / distance-based)

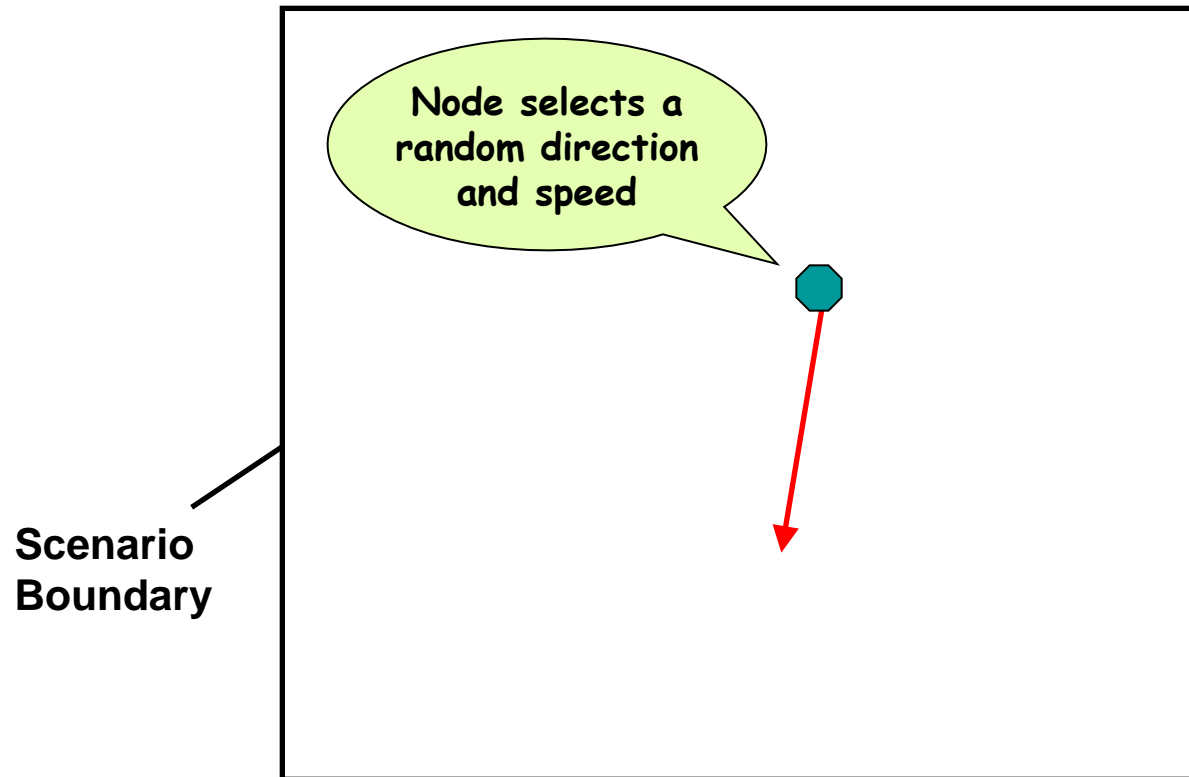
Algorithm:





- Random Walk (time-based / distance-based)

Algorithm:





□ Random Walk (time-based / distance-based)

Algorithm:

Step 1: Select a random speed $speed \in [speed_{Min}; speed_{Max}]$

Step 2: Select a random direction $direction \in [0; 2\pi]$

Step 3: Move into that direction
a. for a pre-defined period of time
b. for a certain distance
c. if the border of the scenario is reached,
select a new direction (bouncing rule)

Step 4: Wait a random period of time $pause \in [0; pause_{Max}]$

Step 5: Go to step 1



□ Random Walk (time-based)

- Characteristics (time-based):
 - Node density (almost) uniform distributed
 - Nodes in are affected by the applied bouncing rule
 - Node speed uniform distributed

- Advantage:
 - Simple to implement
 - Uniform distributed node density (depends on the bouncing rule)

- Disadvantage:
 - Has to be configured carefully
 - Minimum speed
 - Pause duration
 - Travel duration
 - Affected by the bouncing rule
 - Required computational power depends on the movement duration



□ Random Walk (distance-based)

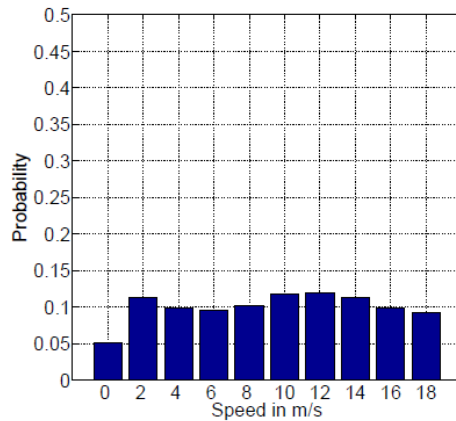
- Characteristics (distance-based):
 - Node density (almost) uniform distributed
 - Nodes in the corner are affected by the applied bouncing rule
 - Node speed decreases over time (similar to RWP)
 - ⇒ Speed decay problem
- Advantage:
 - Simple to implement
 - Uniform distributed node density (depends on the bouncing rule)
- Disadvantage:
 - Has to be configured carefully
 - Minimum speed
 - Pause duration
 - Travel distance
 - Movement affected by the shape of the simulation plane
 - Required computational power depends on the travel distance



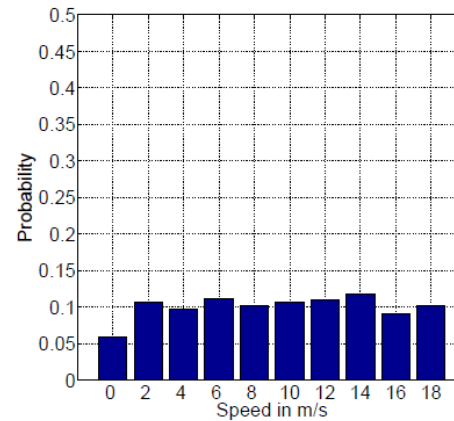
□ Random Walk (time-based)

- Node speed distribution:

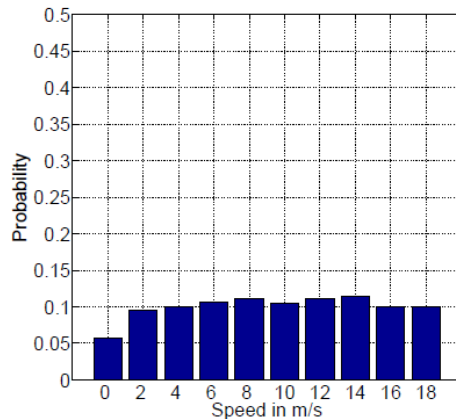
$speed_{Min}$	1 m/s
$speed_{Max}$	20 m/s
$pause_{Min}$	0 s
$pause_{Max}$	0 s
Movement	time-based
Movement Duration	10 s



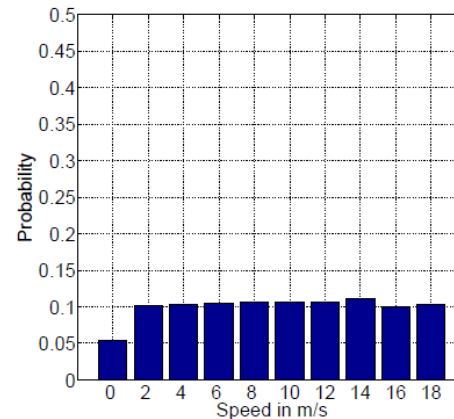
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds



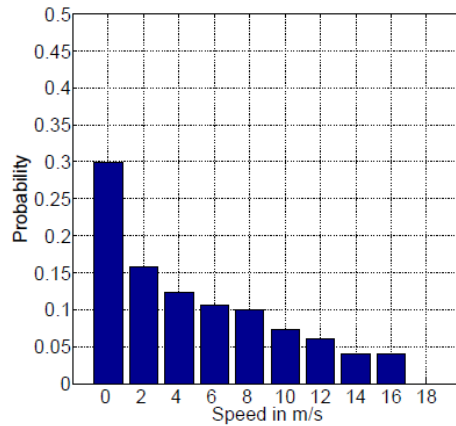
(d) 800 Seconds



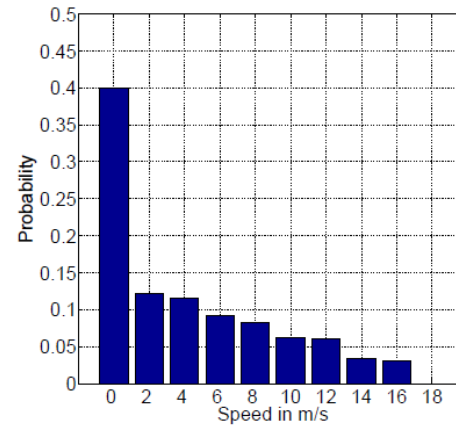
□ Random Walk (distance-based)

- Node speed distribution:

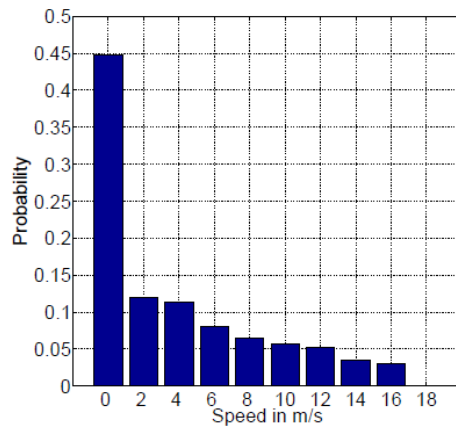
$speed_{Min}$	1 m/s
$speed_{Max}$	20 m/s
$pause_{Min}$	0 s
$pause_{Max}$	0 s
Movement	distance-based
Travel Distance	200 m



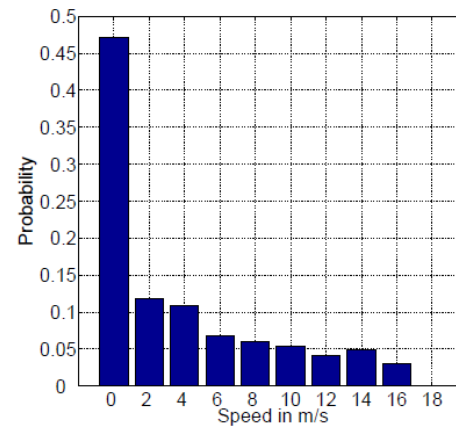
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds



(d) 800 Seconds

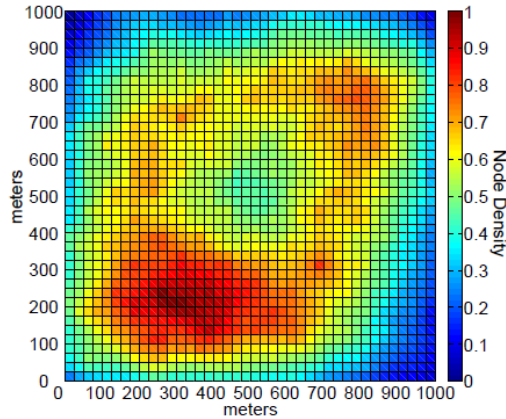


Mobility

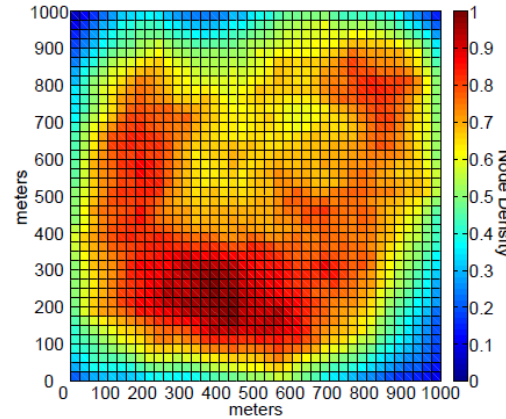
□ Random Walk (time-based)

- Node density:

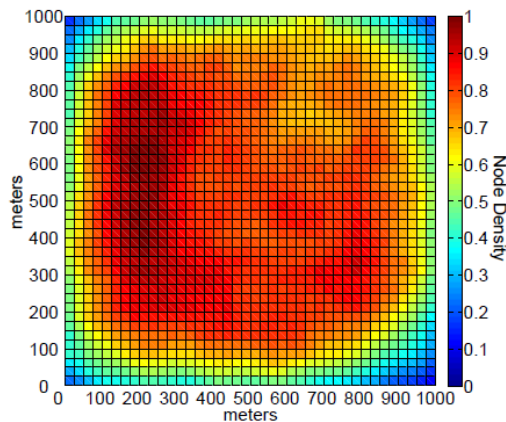
$speed_{Min}$	1 m/s
$speed_{Max}$	20 m/s
$pause_{Min}$	0 s
$pause_{Max}$	0 s
Movement	time-based
Movement Duration	10 s



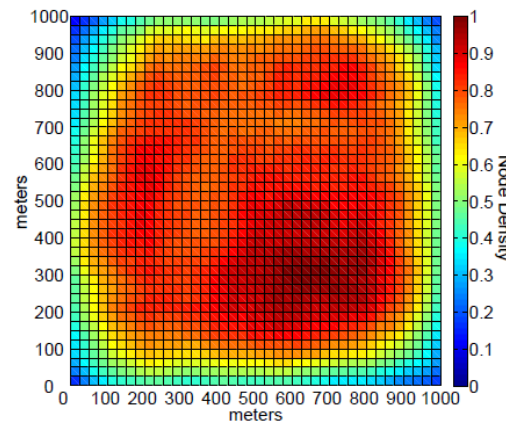
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds



(d) 800 Seconds

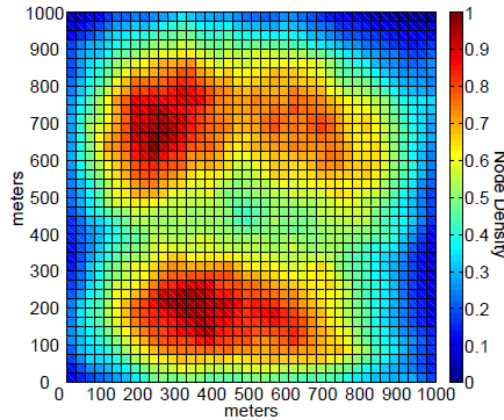


Mobility

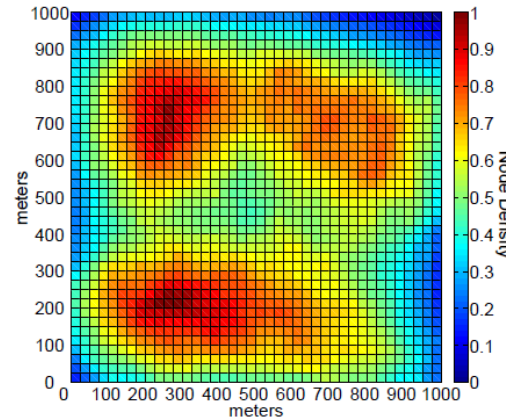
□ Random Walk (distance-based)

- Node density:

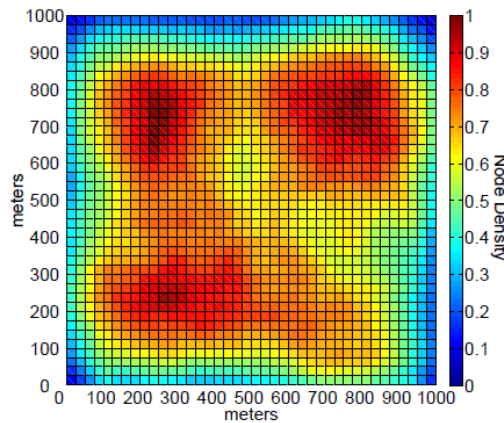
$speed_{Min}$	1 m/s
$speed_{Max}$	20 m/s
$pause_{Min}$	0 s
$pause_{Max}$	0 s
Movement	distance-based
Travel Distance	200 m



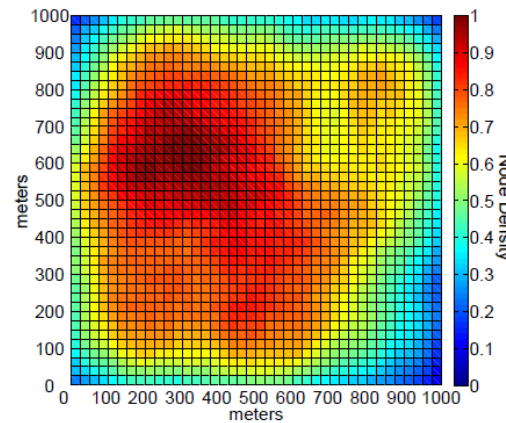
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds



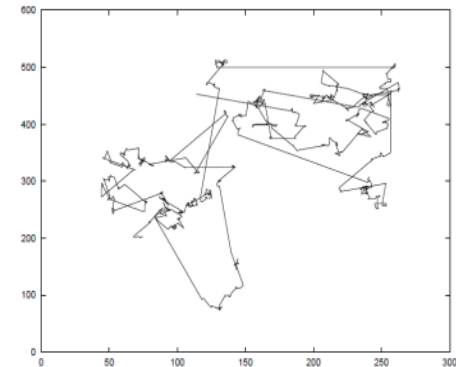
(d) 800 Seconds



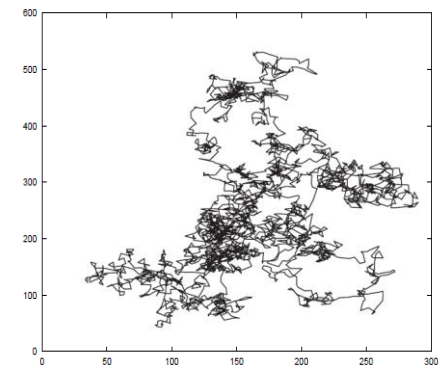
□ Random Walk

- Lévy flight
 - Distance-based random walk
 - Distance is chosen according to a heavy-tailed distribution
 - Probability is high that the object only moves a short distance
 - Probability is low that the object moves straight over a long distance
 - Often used to simulate the movement of humans and animals

- Brownian Motion
 - Distance-based random walk
 - Travel distance between subsequent points is close to zero
 - Describes the movement of small particles in liquids



Example: Lévy flight



Example: Brownian Motion

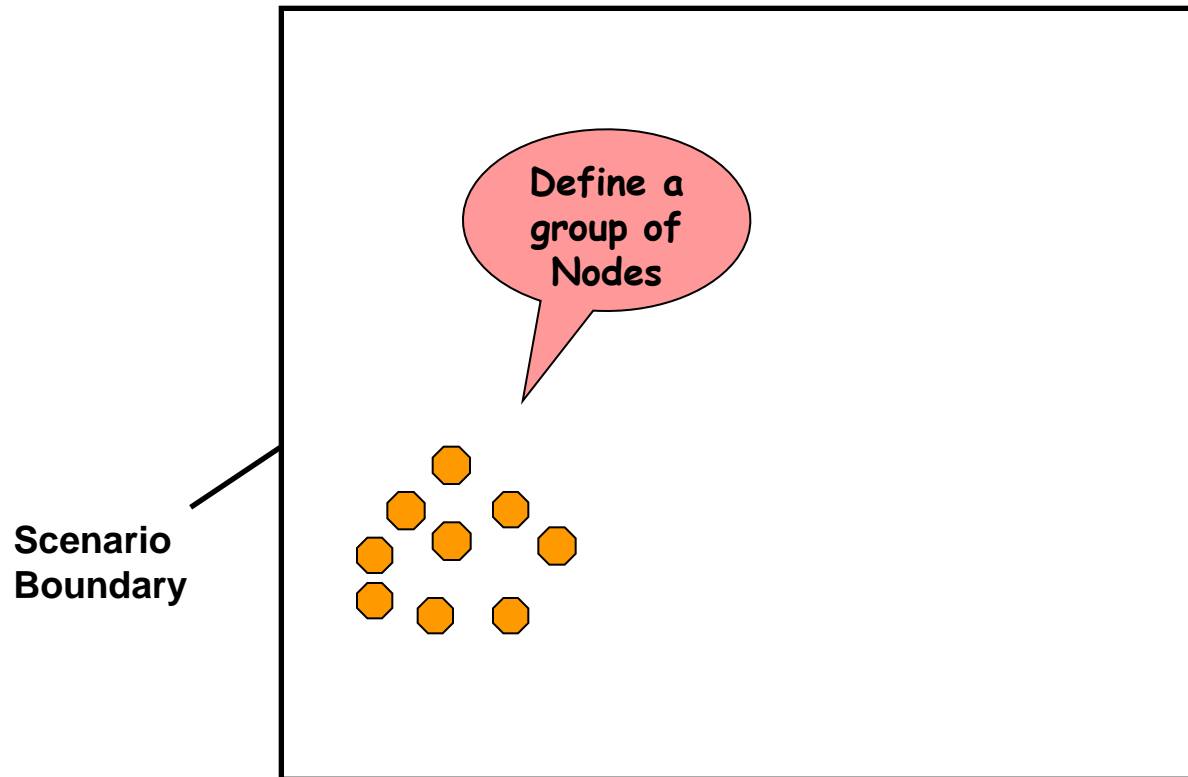


- **Random Walk** (according to Turchin)
 - **Uncorrelated random walk:**
 - Previous move does not affect the following move
 - Each move is independent from the previous one
 - **Correlated random walk:**
 - Previous move affects the following move
 - High probability of moving into the same direction
 - Long travels are followed by short travels with high probability
 - **Biased random walk:**
 - The probability of moving in a certain direction is higher than moving into other directions (non-uniform selection of the direction)
 - **Biased correlated random walk:**
 - Each move is affected by the previous one and an absolute direction
 - **Constrained random walk:**
 - Measured parameters and estimated distributions are used as input for the synthetic mobility model
 - The direction and speed are chosen with respect to the measurements



□ Random Group Mobility

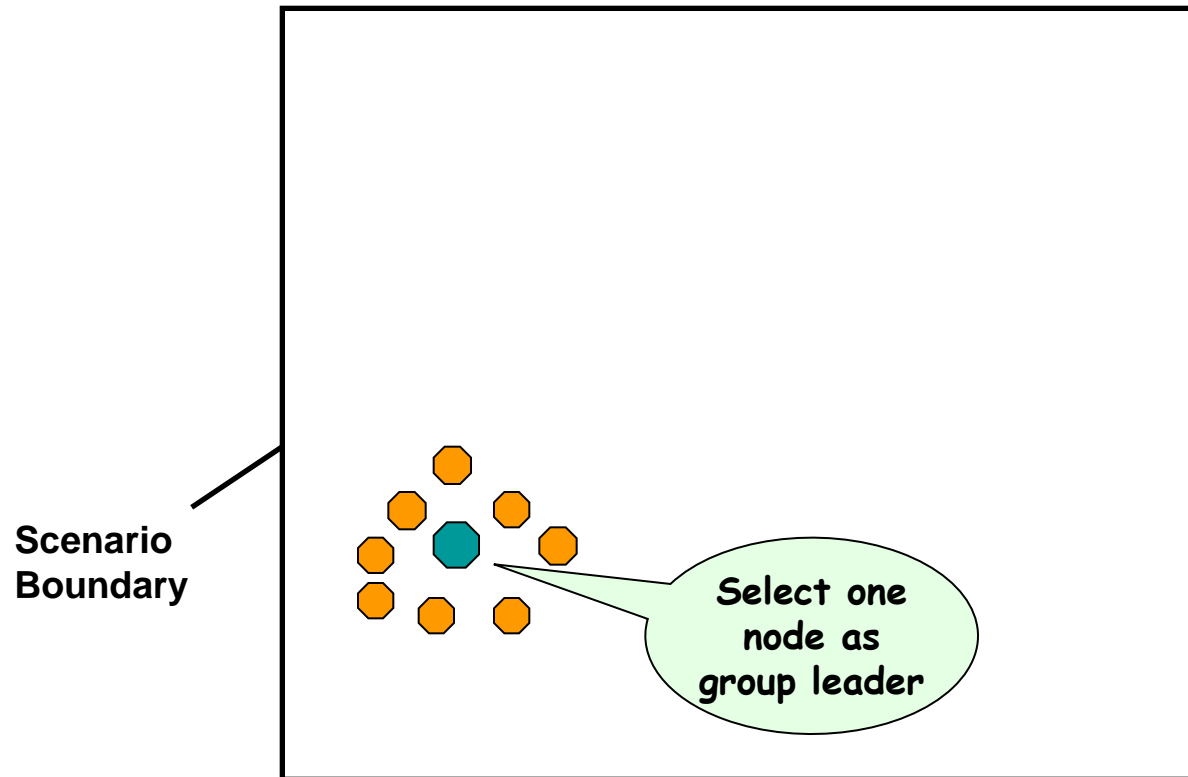
Algorithm:





□ Random Group Mobility

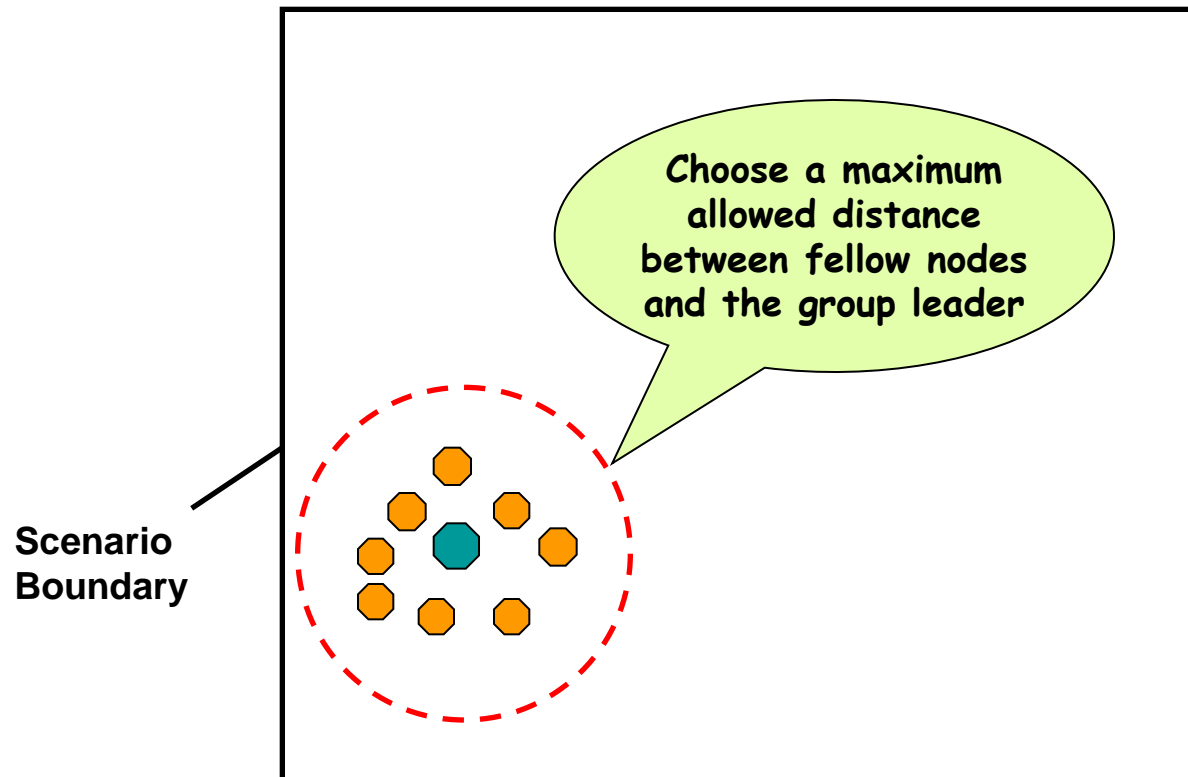
Algorithm:





□ Random Group Mobility

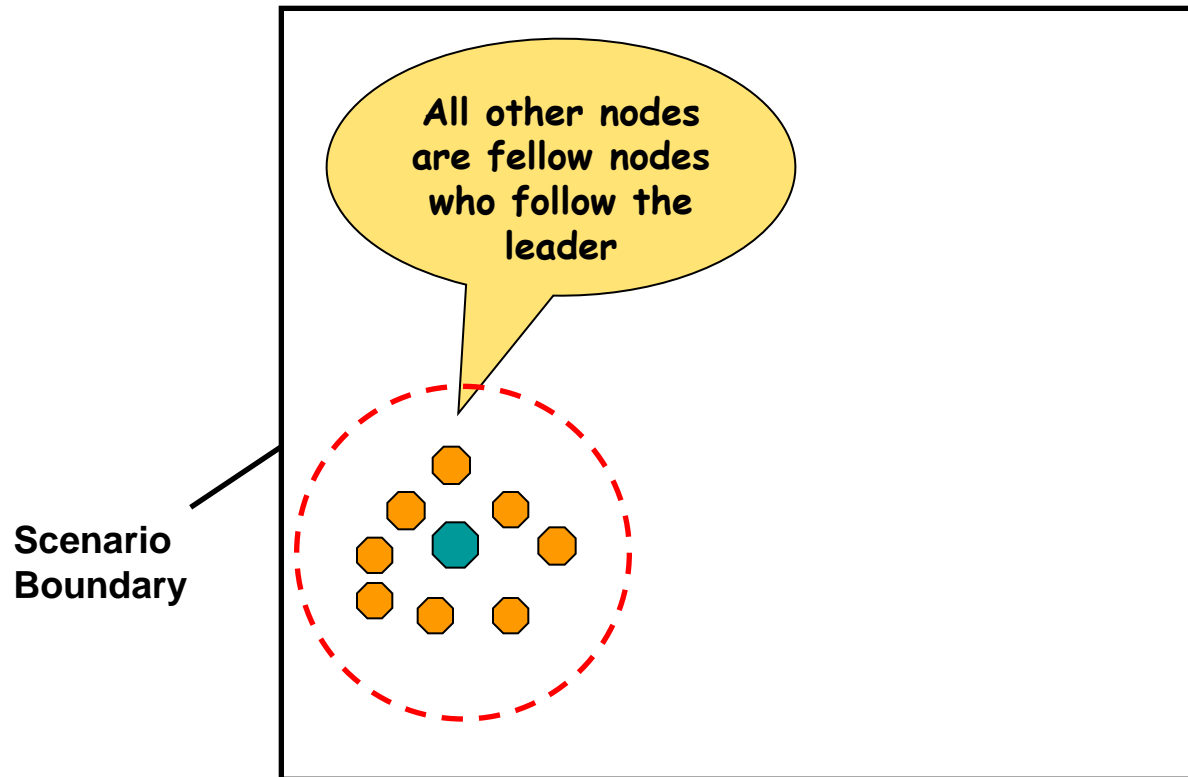
Algorithm:





□ Random Group Mobility

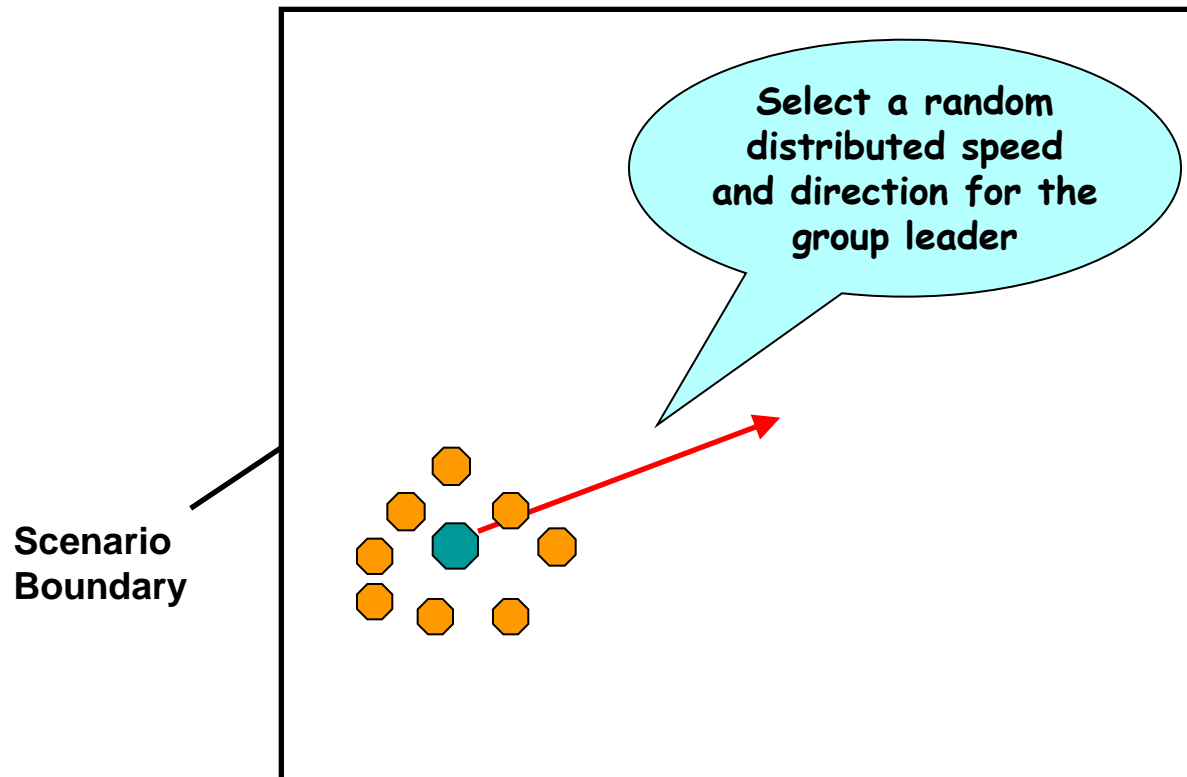
Algorithm:





□ Random Group Mobility

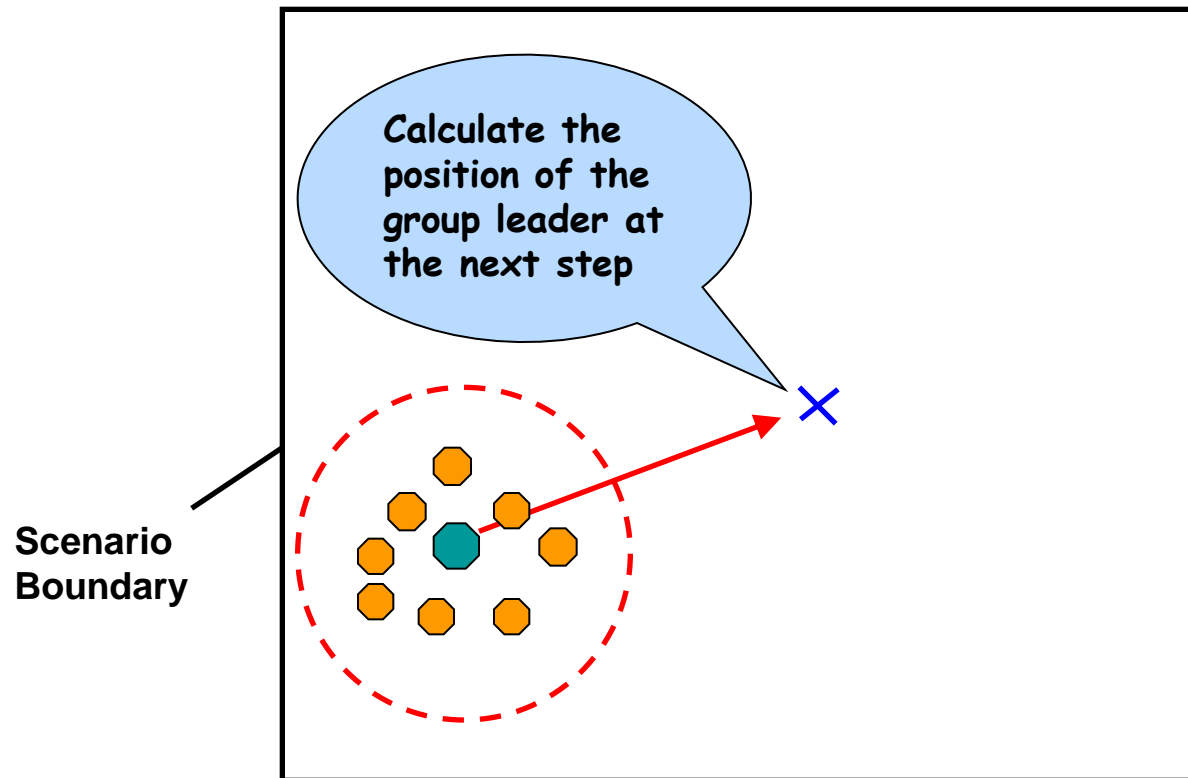
Algorithm:





□ Random Group Mobility

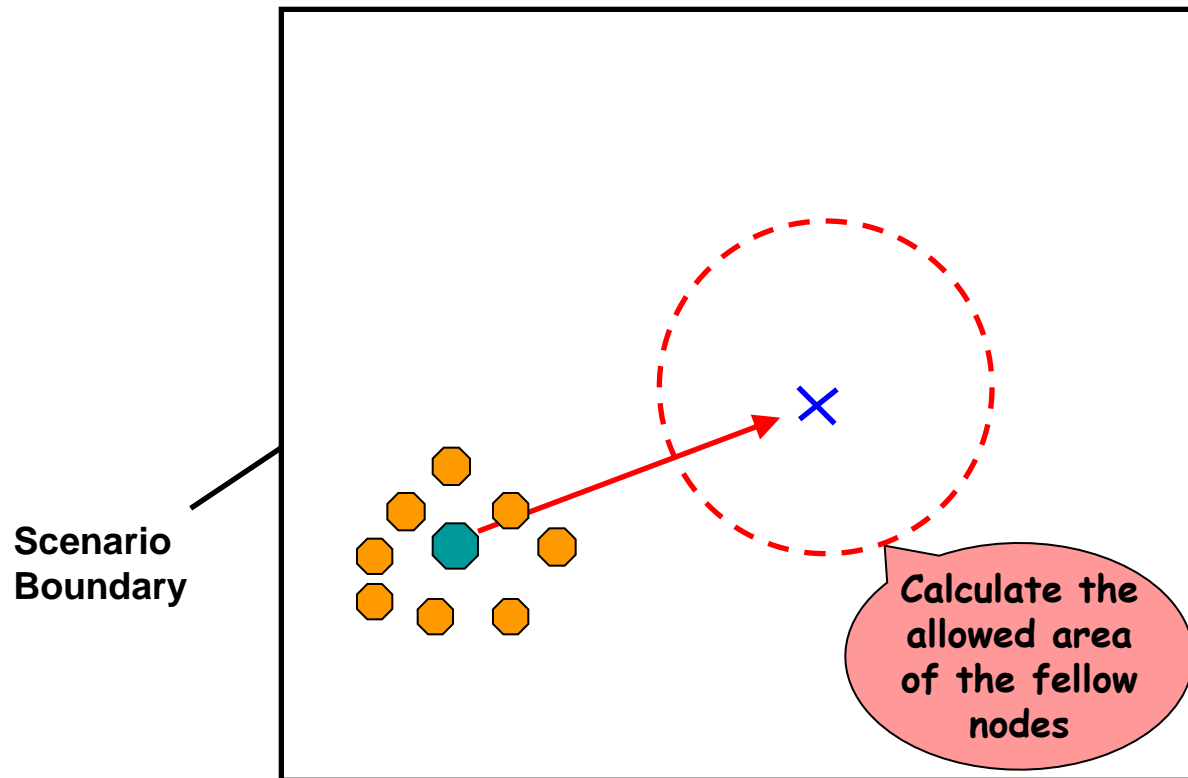
Algorithm:





□ Random Group Mobility

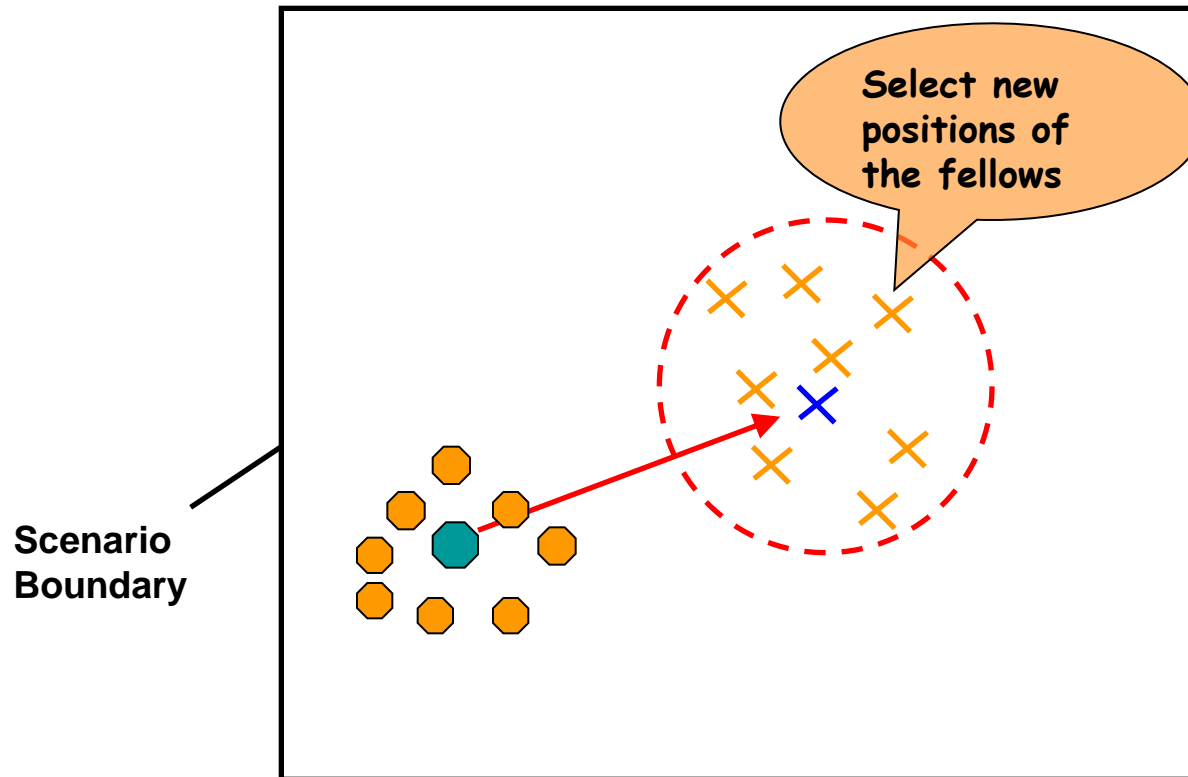
Algorithm:





□ Random Group Mobility

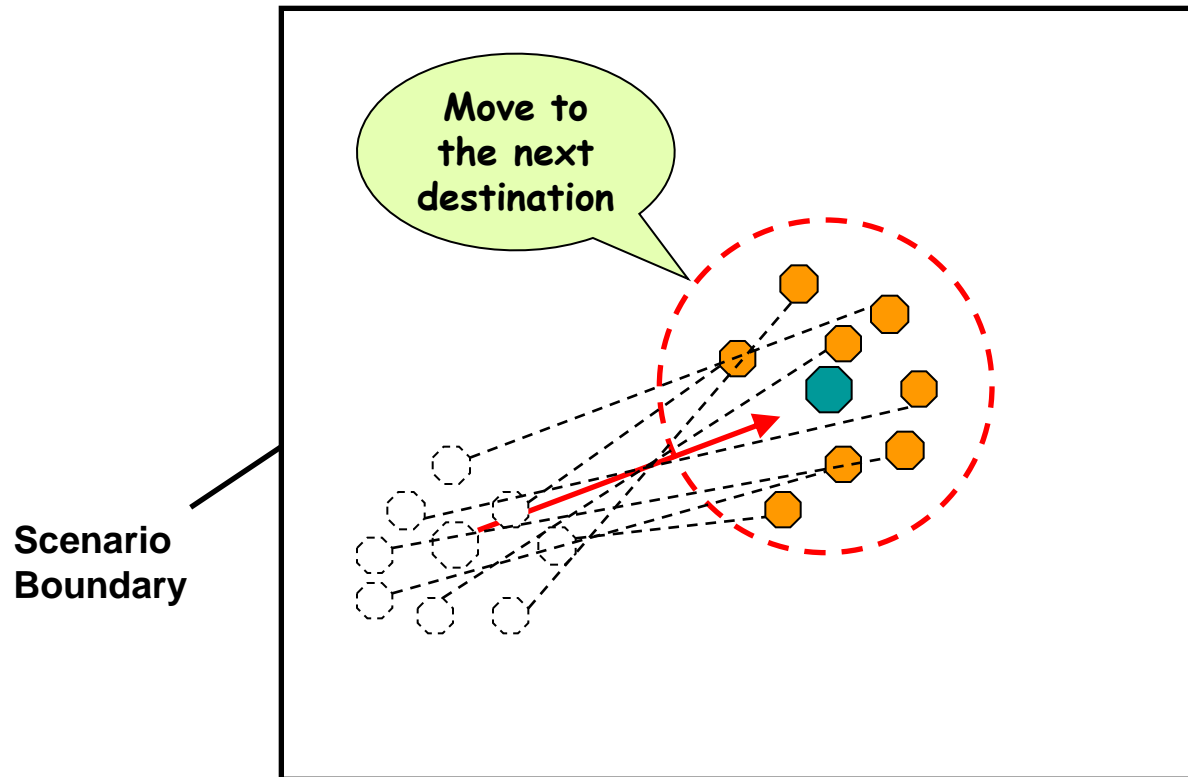
Algorithm:





□ Random Group Mobility

Algorithm:





□ Random Group Mobility

Algorithm (1/2):

Preliminary steps

- Step 1: Define a group of nodes
- Step 2: Select one node as group leader and mark the others as fellows
- Step 3: Choose the maximum allowed distance between a fellow node and the group leader

Group leader

- Step 4: Select a random speed $speed \in [speed_{Min}; speed_{Max}]$
- Step 5: Select a random direction $direction \in [0; 2\pi]$
- Step 6: Go to step 10
- Step 7: Move into that direction
 - a. for a pre-defined period of time / remaining movement duration
 - b. for a pre-defined distance
 - c. Go to step 15 if the border of the scenario is reached before the movement is complete
- Step 8: Wait a random period of time $pause \in [0; pause_{Max}]$
- Step 9: Go to step 4



□ Random Group Mobility

Algorithm (2/2):

Fellow nodes

- Step 10: Calculate the position of the group leader at the next movement / bouncing position
- Step 11: Calculate the allowed area around the group leader at the next movement / bouncing position
- Step 12: Choose a random position within the allowed area
- Step 13: Calculate speed and direction such that the new position is reached at the same time the group leader reaches its next movement / bouncing position
- Step 14: Go to step 7

Group leader

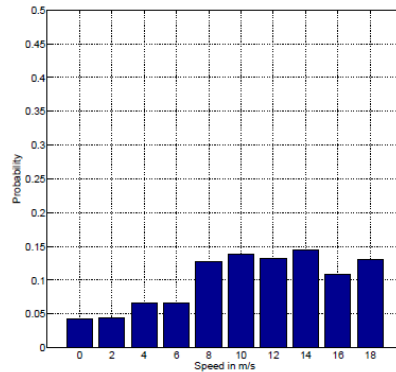
- Step 15: Select a new direction of the group leader
- Step 16: Go to step 10



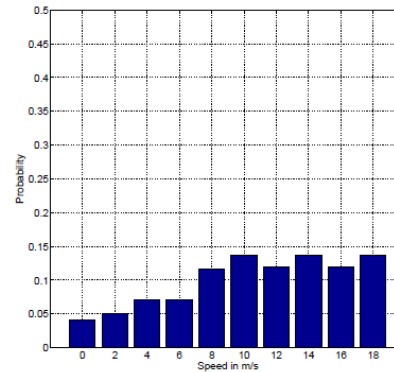
□ Random Group Mobility

- Node speed distribution:

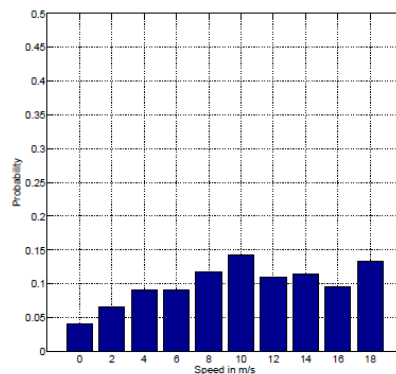
Leader Mobility	Random Walk(time-based)
Leader-Fellow Distance	< 200m
Fellow Area	circle
speed _{Min}	5 m/s
speed _{Max}	20 m/s
pause _{Max}	0 s
Movement Duration	20 s



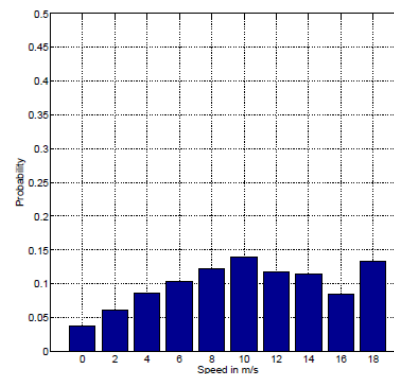
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds



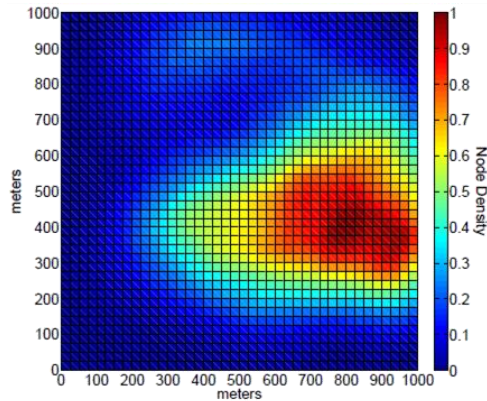
(d) 800 Seconds



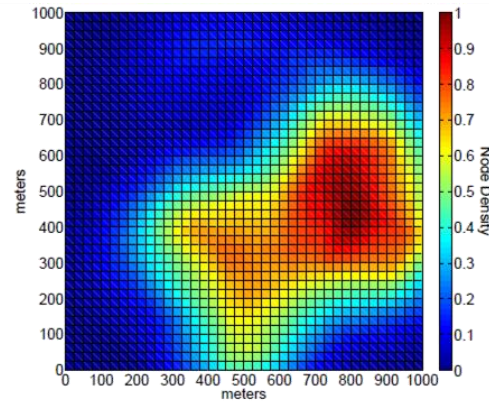
□ Random Group Mobility

- Node density:

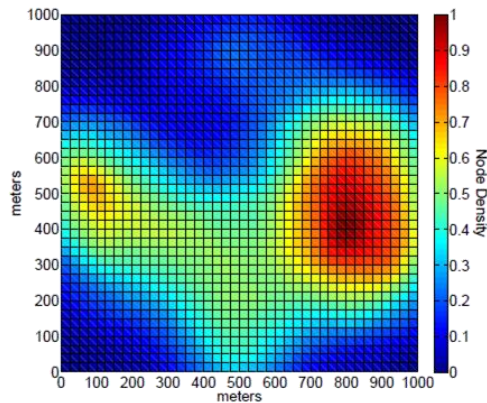
Leader Mobility	Random Walk(time-based)
Leader-Fellow Distance	< 200m
Fellow Area	circle
speed $_{Min}$	5 m/s
speed $_{Max}$	20 m/s
pause $_{Max}$	0 s
Movement Duration	20 s



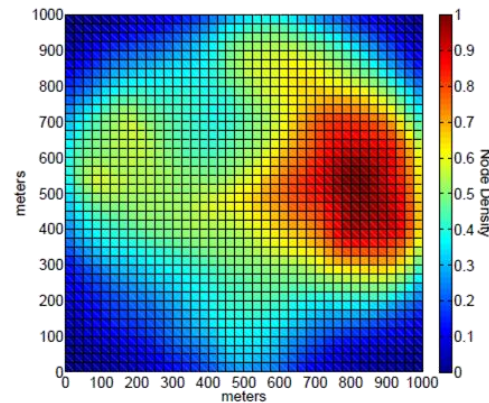
(a) 100 Seconds



(b) 200 Seconds



(c) 400 Seconds

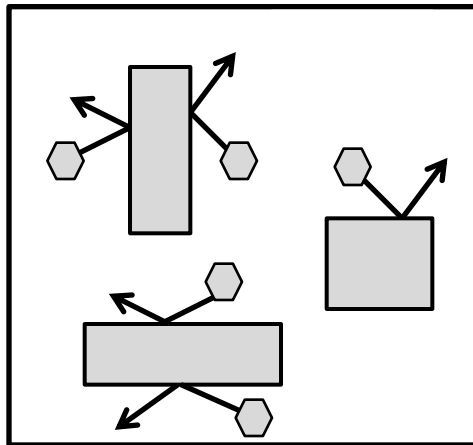


(d) 800 Seconds

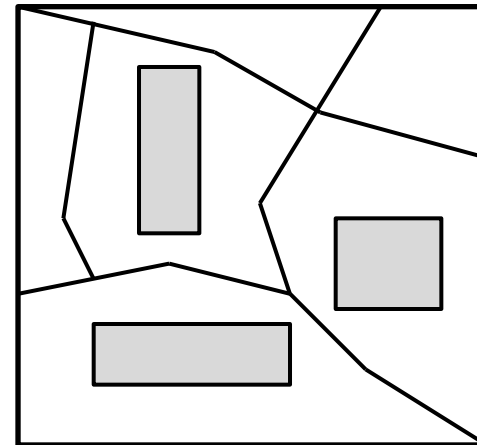


□ Obstacles:

- Movement of objects is usually constraint by
 - obstacles
 - pre-defined pathways
- Bouncing rule becomes more important with an increasing number of obstacles
- Obstacles block movement but do not necessarily affect the signal propagation (e.g. river or lake)
- Some models use Voronoi diagrams as predefined paths



Movement with obstacles



Movement with obstacles and predefined paths



Mobility

□ How to describe position and orientation?

▪ Position:

- Geographic

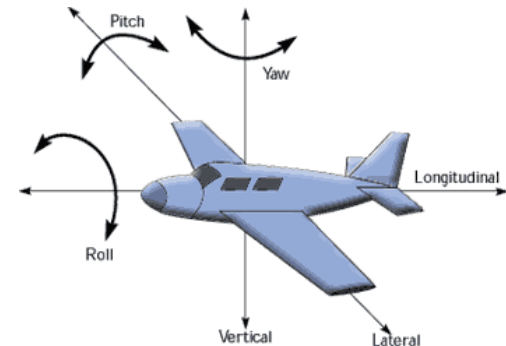
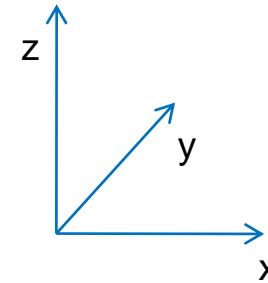
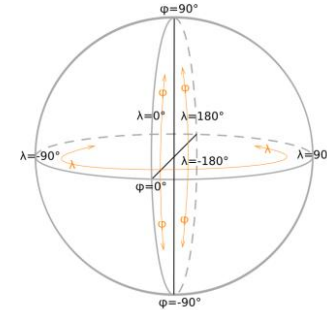
Latitude φ , Longitude λ , Altitude

- Cartesian

X, Y, Z

▪ Orientation:

- Yaw
- Pitch
- Roll



Picture taken from nasa.gov



□ Implementation:

▪ Types of mobility

- Direct
 - Change the position and orientation of objects directly at a given simulation time
- Trajectory
 - Sequence of triples [position, orientation, simulation time] which describe the position and orientation at a given simulation time
 - The movement is usually interpolated between subsequent triples
- Vector
 - Bearing, ground speed, ascent rate
 - Trajectories can be described by [bearing, ground speed, simulation time] triples
- External modification
 - Co-simulation
 - Hardware-In-The-Loop
 - Can use any type of mobility