



Network Security

Chapter 2 Basics of Cryptography

- Overview of Cryptographic Algorithms
- Attacking Cryptographic Algorithms
- Historical Approaches
- Foundations of Modern Cryptography



Cryptographic algorithms: overview

- During this course two main applications of cryptographic algorithms are of principal interest:
 - *Encryption* of data: transforms plaintext data into ciphertext in order to conceal its' meaning
 - *Signing* of data: computes a *check value* or *digital signature* to a given plain- or ciphertext, that can be verified by some or all entities being able to access the signed data
- Some cryptographic algorithms can be used for both purposes, some are only secure and / or efficient for one of them.
- Principal categories of cryptographic algorithms:
 - *Symmetric cryptography* using 1 key for en-/decryption or signing/checking
 - *Asymmetric cryptography* using 2 different keys for en-/decryption or signing/checking
 - *Cryptographic hash functions* using 0 keys (the “key” is not a separate input but “appended” to or “mixed” with the data).



Attacking cryptography (1): Cryptanalysis

- ❑ *Cryptanalysis* is the process of attempting to discover the plaintext and / or the key
- ❑ Types of cryptanalysis:
 - *Ciphertext only*: specific patterns of the plaintext may remain in the ciphertext (frequencies of letters, digraphs, etc.)
 - *Known ciphertext / plaintext pairs*
 - *Chosen plaintext or chosen ciphertext*
 - Newer developments: *differential cryptanalysis, linear cryptanalysis*
- ❑ Cryptanalysis of public key cryptography:
 - The fact that one key is publicly exposed may be exploited
 - Public key cryptanalysis is more aimed at breaking the cryptosystem itself and is closer to pure mathematical research than to classical cryptanalysis
 - Important directions:
 - Computation of discrete logarithms
 - Factorization of large integers



Attacking cryptography (2): brute force attack

- The *brute force attack* tries every possible key until it finds an intelligible plaintext:
 - Every cryptographic algorithm can in theory be attacked by brute force
 - On average, half of all possible keys will have to be tried

Average Time Required for Exhaustive Key Search

Key Size [bit]	Number of keys	Time required at 1 encryption / μs	Time required at 10^6 encryption/ μs
32	$2^{32} = 4.3 * 10^9$	$2^{31} \mu\text{s} = 35.8$ minutes	2.15 milliseconds
56	$2^{56} = 7.2 * 10^{16}$	$2^{55} \mu\text{s} = 1142$ years	10.01 hours
128	$2^{128} = 3.4 * 10^{38}$	$2^{127} \mu\text{s} = 5.4 * 10^{24}$ years	$5.4 * 10^{18}$ years

- 1 encryption / μs : 100 Clock cycles of a 100 MHz processor
- 10^6 encryptions / μs : Clock cycles using 500 parallel 2GHz processors



Attacking cryptography (3): How large is large?

Reference Numbers Comparing Relative Magnitudes

Reference	Magnitude
Seconds in a year	$\approx 3 * 10^7$
Seconds since creation of solar system	$\approx 2 * 10^{17}$
Clock cycles per year (3 GHz computer)	$\approx 1 * 10^{17}$
Binary strings of length 64	$2^{64} \approx 1.8 * 10^{19}$
Binary strings of length 128	$2^{128} \approx 3.4 * 10^{38}$
Binary strings of length 256	$2^{256} \approx 1.2 * 10^{77}$
Number of 75-digit prime numbers	$\approx 5.2 * 10^{72}$
Electrons in the universe	$\approx 8.37 * 10^{77}$



Classification of modern encryption algorithms

- ❑ The type of operations used for transforming plaintext to ciphertext:
 - *Substitution*, which maps each element in the plaintext (bit, letter, group of bits or letters) into another element
 - *Transposition*, which re-arranges elements in the plaintext
- ❑ The number of keys used:
 - *Symmetric ciphers*, which use the same key for en- / decryption
 - *Asymmetric ciphers*, which use different keys for en- / decryption
- ❑ The way in which the plaintext is processed:
 - *Stream ciphers* work on bit streams and encrypt one bit after another
 - *Block ciphers* work on blocks of width b with b depending on the specific algorithm.



Basic Kryptographic Principles

□ Substitution

- Individual characters are exchanged by other characters

Types of substitution

- simple substitution substitution: operates on single letters
- polygraphic substitution: operates on larger groups of letters

- monoalphabetic substitution: uses fixed substitution over the entire message
- polyalphabetic substitution: uses different substitutions at different sections of a message

□ Transposition

- The position of individual characters changes (Permutation)



Transposition: scytale

- Known as early as 7th century BC
- Principle:
 - Wrap parchment strip over a wooden rod of a fixed diameter and write letters along the rod.
 - Unwrap a strip and “transmit”
 - To decrypt, wrap a received over a wooden rod of the same diameter and read off the text.



- Example:

troops
headii
nthewe
stneed
moresu
pplies



thnsm predd opoah nrlod eeeis iedus

- Weakness:
 - Easy to break by finding a suitable matrix transposition.



Monoalphabetic substitution: Atbash

Jeremiah 25:25

And all the kings of the north, far and near, one with another, and all the kingdoms of the world, which are upon the face of the earth: and the king of Sheshach shall drink after them.

Atbash code: reversed Hebrew alphabet.

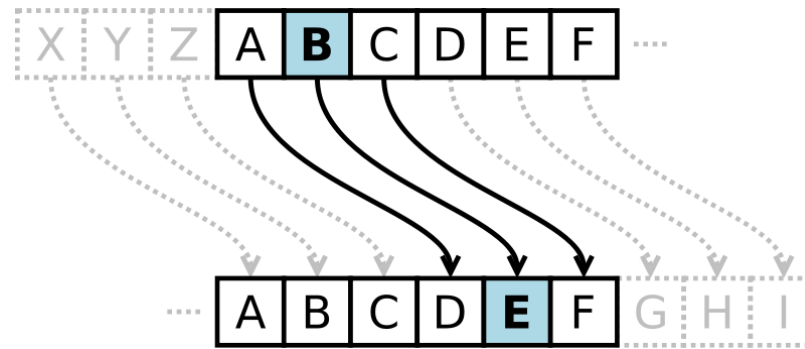
A <u>Aleph</u> א	B <u>Beth</u> ב	G <u>Gimel</u> ג	D <u>Daleth</u> ד	H <u>He</u> ה	WV FY <u>Waw</u> ו	Z <u>Zajin</u> ז	H <u>Chet</u> ח	T <u>Tet</u> ט	IJ <u>Jod</u> י	K <u>Kaph</u> כך	L <u>Lamed</u> ל	M <u>Mem</u> מם	N <u>Nun</u> נן	X <u>Samech</u> ס	O <u>Ajin</u> ע	P <u>Pe</u> פף	Z <u>Sade</u> צץ	Q <u>Koph</u> ק	R <u>Resch</u> ר	S <u>Sin</u> ש	T <u>Taw</u> ת
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Sheshach ⇒ ש ש כ ⇒ ל ב ⇒ Babel



Monoalphabetic substitution: Caesar cipher

- Caesar code: left shift of alphabet by 3 positions.



- Example (letter of Cicero to Caesar):

MDEHV RSNQNRQNV PHDH XHVXNPRQNZP

HABES OPINIONIS MEAE TESTIMONIUM

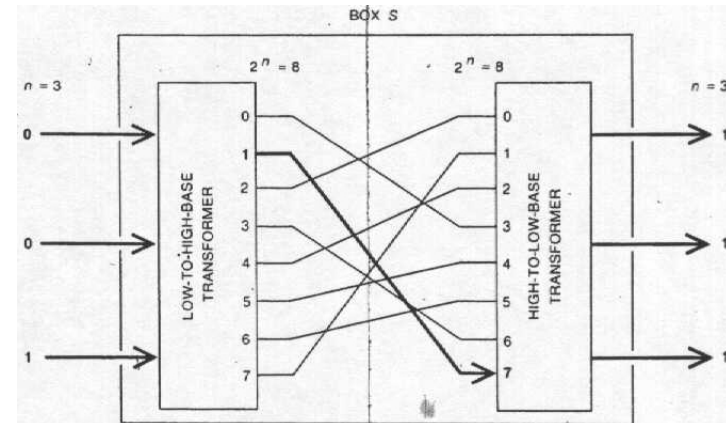
- Weakness: a limited number of possible substitutions. Easy to break by brute force!



Modern cryptography: S and P-boxes

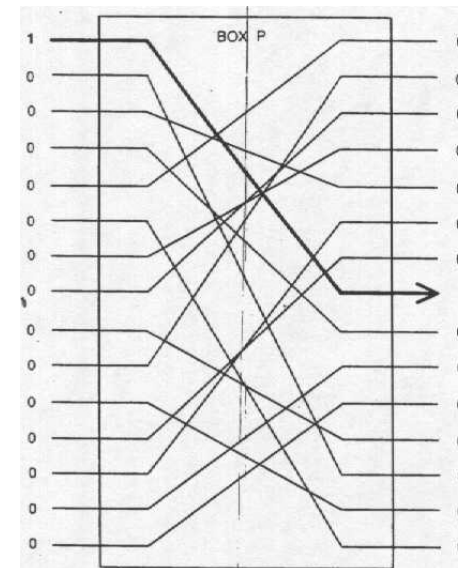
S-box:

- ❑ Block-wise **substitution** of binary digits.
- ❑ Resistant to attacks for sufficiently large block size; e.g. for $n=128$ it provides 2^{128} possible mappings.



P-box:

- ❑ Block-wise **permutation** of binary digits.
- ❑ Realizes a simple **transposition** cipher with maximal entropy.
- ❑ Problem: straightforward attacks exist.





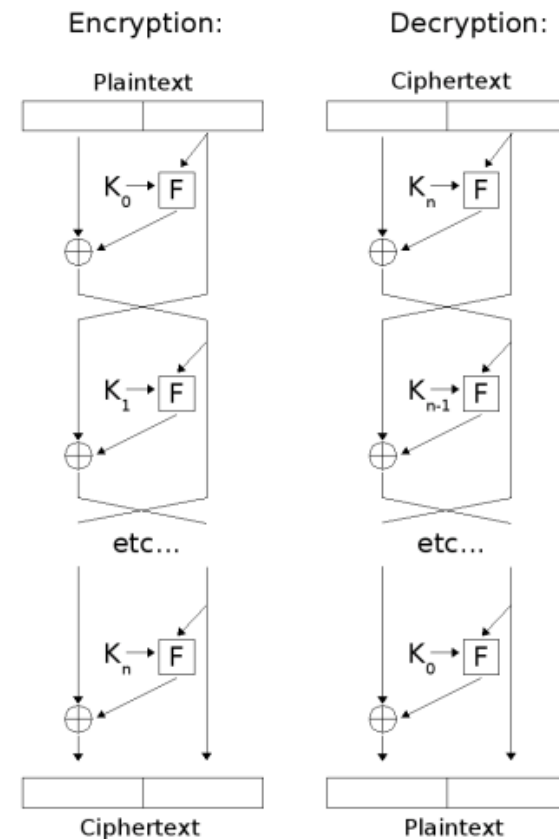
Feistel network: a product cipher of S and P-boxes

- ❑ A revival of the idea of a product cipher.
- ❑ Multiple rounds provide a cryptographically strong polyalphabetic substitution.
- ❑ Combination of substitution with transposition provides protection against specific attacks (frequency analysis).
- ❑ Follows the theoretical principles outlined by C. Shannon in 1949: combines “confusion” with “diffusion” to attain maximal entropy of a cipher text.
 - Confusion: cipher text statistics depend in a very complex way on plaintext statistics (approach: substitution in different rounds)
 - Diffusion: each digit in plaintext and in key influence many digits of cipher text (approach: many rounds with transposition)



A practical Feistel cipher

- ❑ A multiple-round scheme with separate keys per round.
- ❑ Invertible via a reverse order of rounds.
- ❑ 3 rounds suffice to achieve a pseudorandom permutation.
- ❑ 4 rounds suffice to achieve a strong pseudorandom permutation (i.e. it remains pseudorandom to an attacker with an oracle access to its inverse permutation).
- ❑ A foundation for a large number of modern symmetric ciphers: DES, Lucifer, Blowfish, RC5, Twofish, etc.



Feistel Cipher



Important properties of encryption algorithms

Consider, a sender is encrypting plaintext messages P_1, P_2, \dots to ciphertext messages C_1, C_2, \dots

Then the following properties of the encryption algorithm are of special interest:

- *Error propagation* characterizes the effects of bit-errors during transmission of ciphertext to reconstructed plaintext P_1', P_2', \dots
 - Depending on the encryption algorithm there may be one or more erroneous bits in the reconstructed plaintext per erroneous ciphertext bit

- *Synchronization* characterizes the effects of lost ciphertext data units to the reconstructed plaintext
 - Some encryption algorithms can not recover from lost ciphertext and need therefore explicit re-synchronization in case of lost messages
 - Other algorithms do automatically re-synchronize after 0 to n (n depending on the algorithm) ciphertext bits



Cryptographic algorithms: outline

